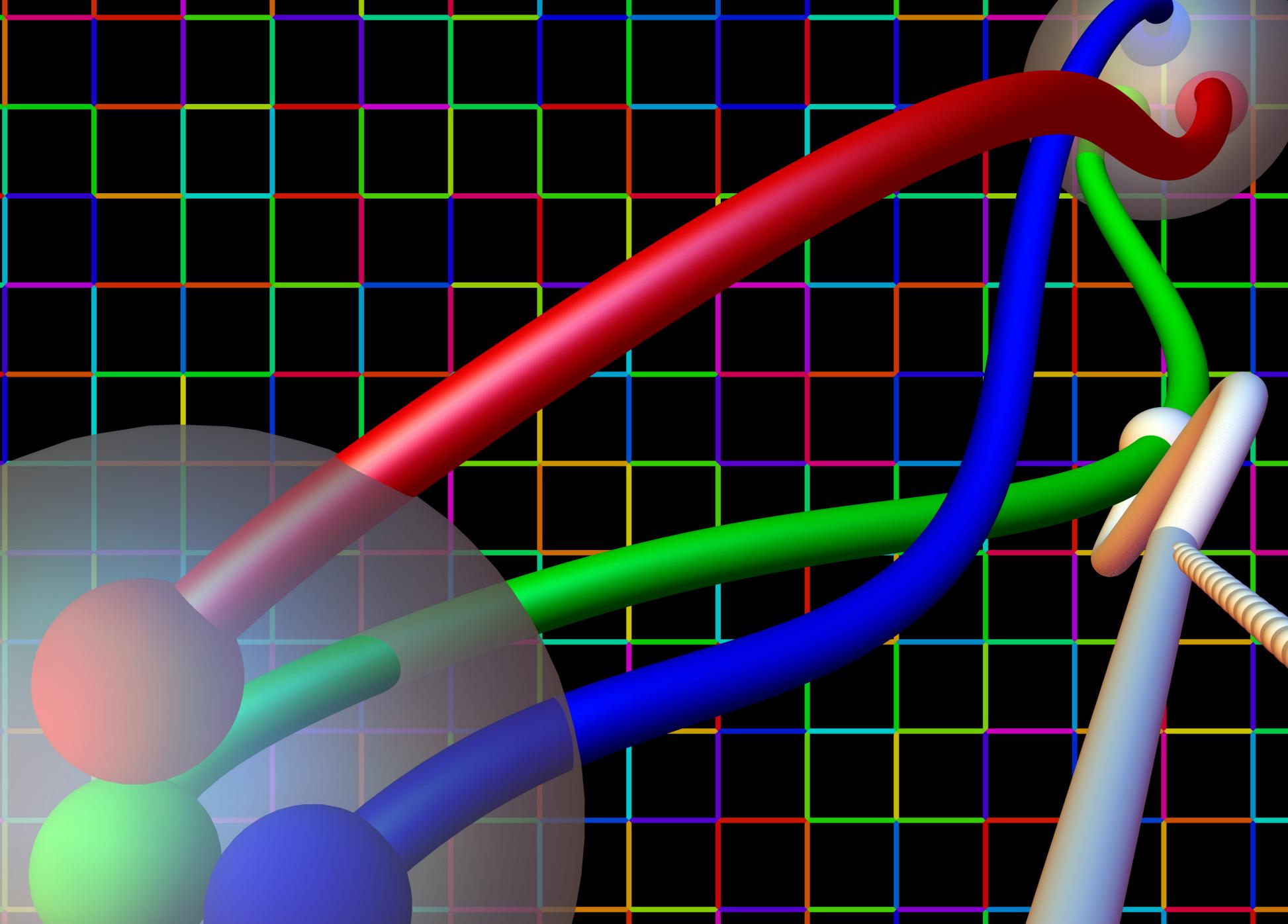


Understanding Fundamental Symmetries with Lattice QCD



Evan Berkowitz
College of Science and Mathematics
University of the Virgin Islands

UT Knoxville Colloquium
2025 January 30



Fundamental Symmetries

The Standard Model

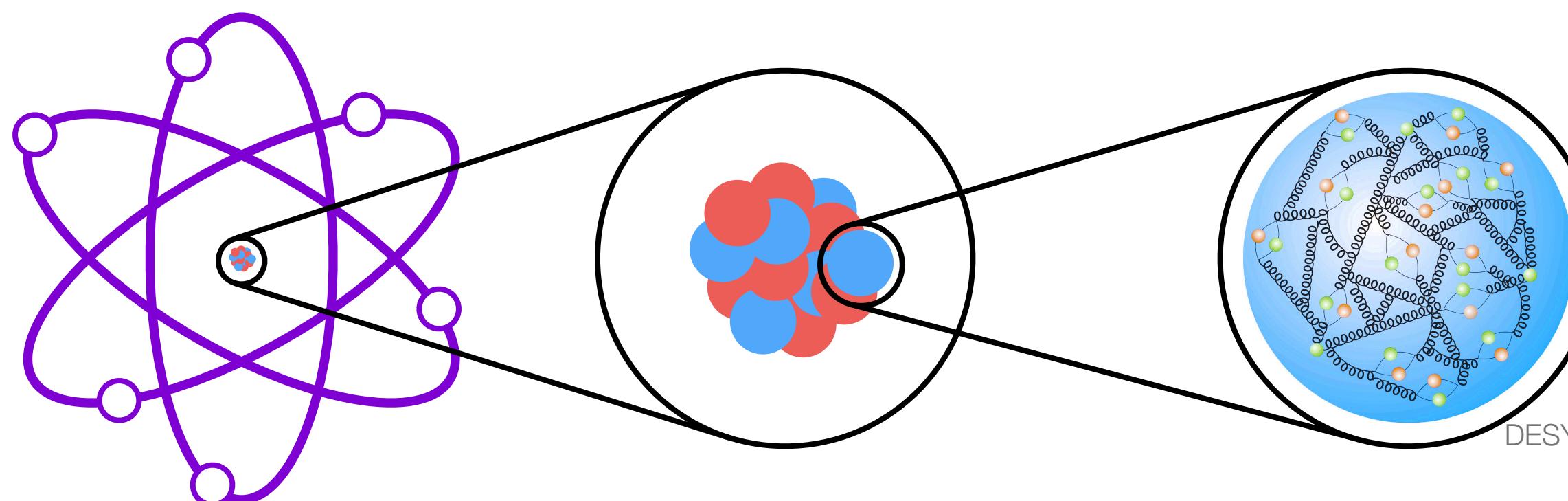
- A *quantum field theory* with particular symmetries.
- No gravity, neutrino masses and oscillations, dark matter
- Otherwise, the ultimate description of every physical phenomenon thus far observed!

Baryon number is conserved.

Lepton number is conserved!

QUARKS	mass \rightarrow	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
	charge \rightarrow	2/3	2/3	2/3	0	0
	spin \rightarrow	1/2	1/2	1/2	1	0
u					g	
c						H
t						
d	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$		γ	
s	-1/3	-1/3	-1/3			
b	1/2	1/2	1/2			
electron	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²		Z	
muon	-1	-1	-1			
tau	1/2	1/2	1/2			
ν_e	<2.2 eV/c ²	<0.17 MeV/c ²	<15.5 MeV/c ²		W	
electron neutrino	0	0	0			
ν_μ	1/2	1/2	1/2			
muon neutrino						
ν_τ						
tau neutrino						
W boson	80.4 GeV/c ²	91.2 GeV/c ²	105.7 MeV/c ²			
	± 1	0	1			
	1	1	1			

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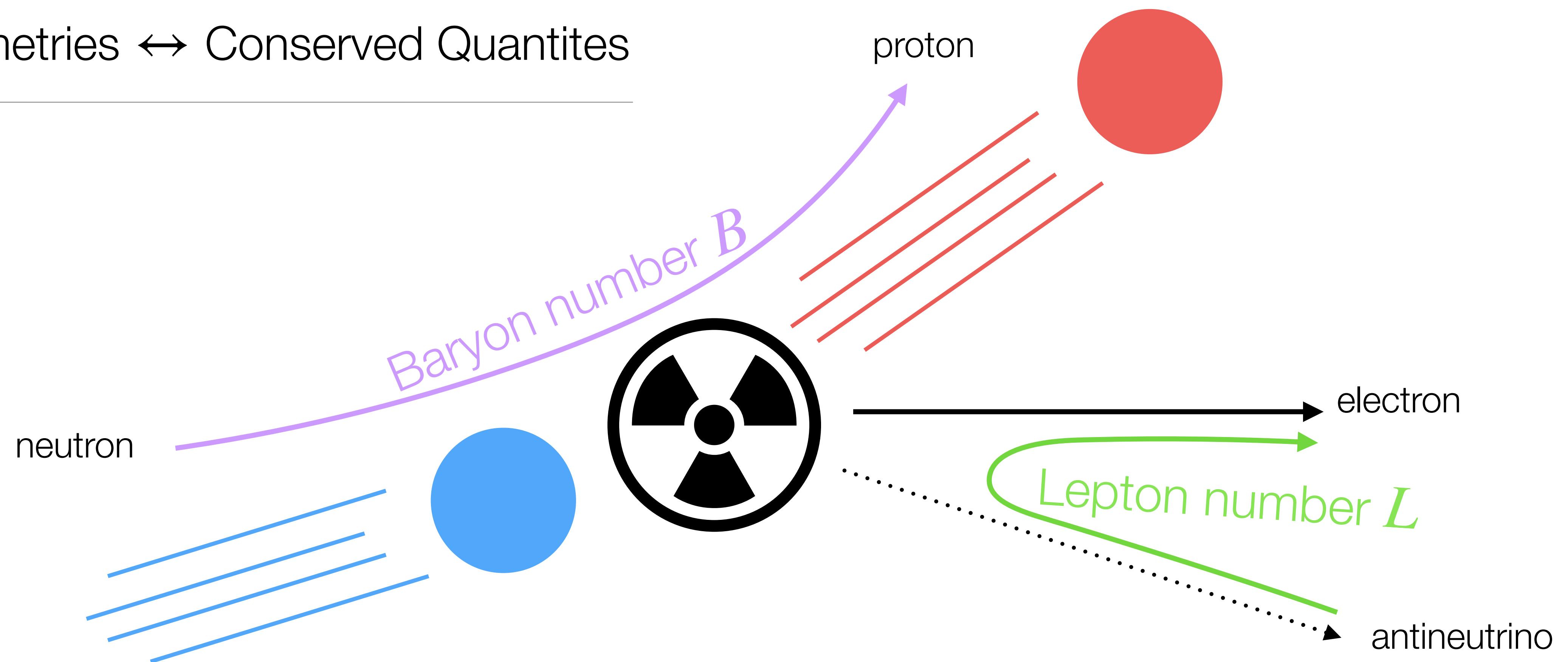


Atomic Scale
 $(25 \text{ to } 250) \times 10^{-12} \text{ m}$

Nuclear Scale
 $(1 \text{ to } 10) \times 10^{-15} \text{ m}$

Proton / Neutron Scale
 $1 \times 10^{-15} \text{ m}$

Symmetries \leftrightarrow Conserved Quantities



$$\begin{array}{ccccccc} n & \rightarrow & p & + & e^- & + & \bar{\nu} \\ B: 1 & = & 1 & + & 0 & + & 0 \\ L: 0 & = & 0 & + & 1 & + & (-1) \end{array}$$

Symmetries of the Standard Model

- Time invariance
- Rotational invariance
- Translational invariance
- P: Parity
- C: Charge conjugation
- T: Time reversal
- $SU(3) \times SU(2) \times U(1)$
- Baryon, Lepton number conservation

continuous spacetime symmetries

discrete spacetime symmetries?

	mass \rightarrow	charge \rightarrow	spin \rightarrow	
QUARKS				
u	$\approx 2.3 \text{ MeV}/c^2$	2/3	1/2	up
c	$\approx 1.275 \text{ GeV}/c^2$	2/3	1/2	charm
t	$\approx 173.07 \text{ GeV}/c^2$	2/3	1/2	top
g	0	0	1	gluon
H	$\approx 126 \text{ GeV}/c^2$	0	0	Higgs boson
d	$\approx 4.8 \text{ MeV}/c^2$	-1/3	1/2	down
s	$\approx 95 \text{ MeV}/c^2$	-1/3	1/2	strange
b	$\approx 4.18 \text{ GeV}/c^2$	-1/3	1/2	bottom
γ	0	0	1	photon
e	0.511 MeV/c^2	-1	1/2	electron
μ	105.7 MeV/c^2	-1	1/2	muon
τ	1.777 GeV/c^2	-1	1/2	tau
Z	91.2 GeV/c^2	0	1	Z boson
ν_e	<2.2 eV/c^2	0	1/2	electron neutrino
ν_μ	<0.17 MeV/c^2	0	1/2	muon neutrino
ν_τ	<15.5 MeV/c^2	0	1/2	tau neutrino
W	80.4 GeV/c^2	± 1	1	W boson
GAUGE BOSONS				

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gauge symmetry

accidental symmetries?

Parity

Case study: Parity (mid-1950s)

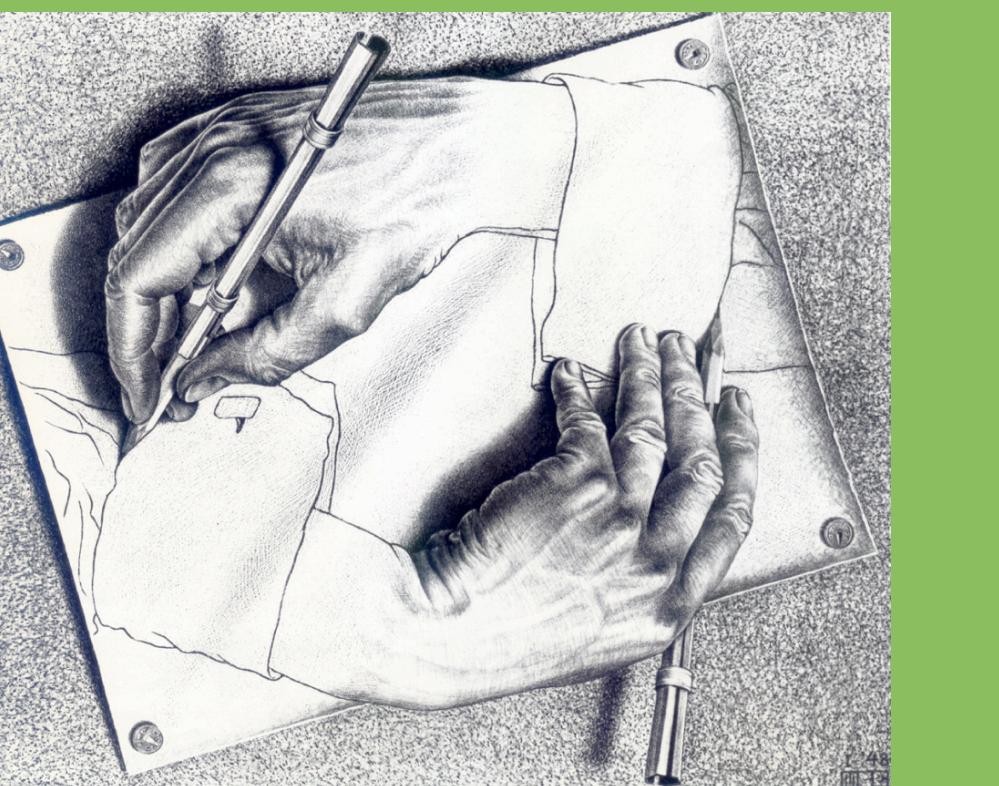
$$\theta^+ \rightarrow \pi^+ + \pi^0$$

$$\tau^+ \rightarrow \pi^+ + \pi^+ + \pi^-$$

- Measurements showed θ and τ had indistinguishable mass, lifetimes, ...
- But pions π had negative parity, so θ^+ and τ^+ must have opposite parity, because parity is conserved.
- So what could explain the degeneracy?

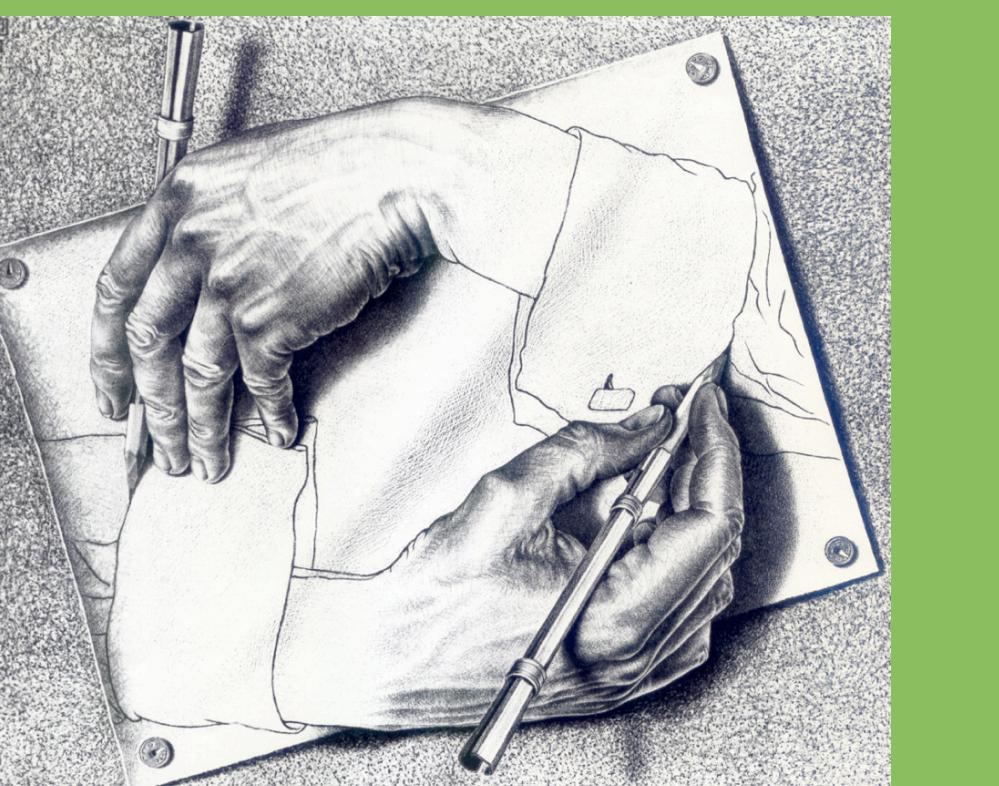


Case study: Parity



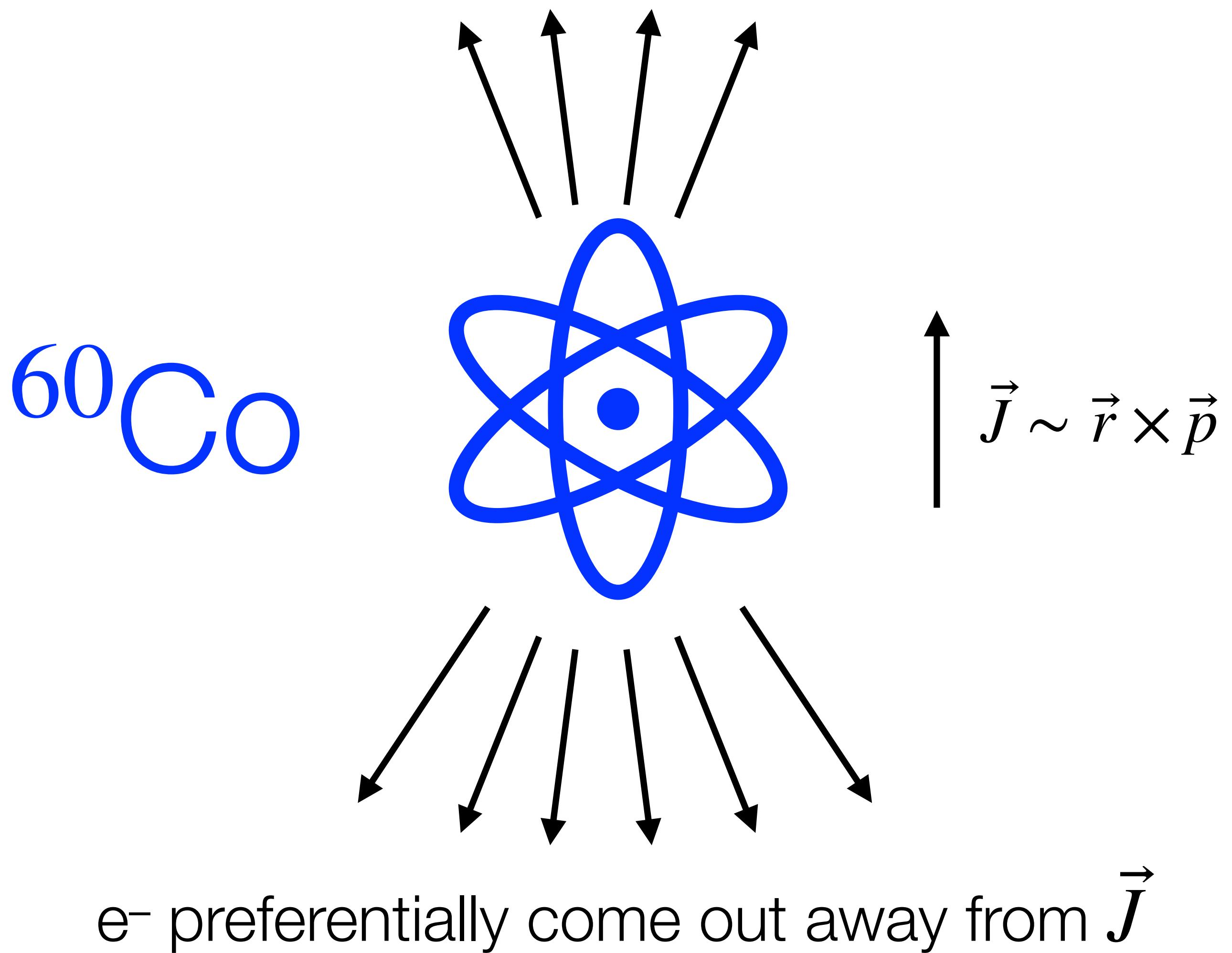
MC Escher

$$P \neq \bar{P}$$



Chien-shiung Wu (1912-1997)
Smithsonian Institution

Case study: Parity

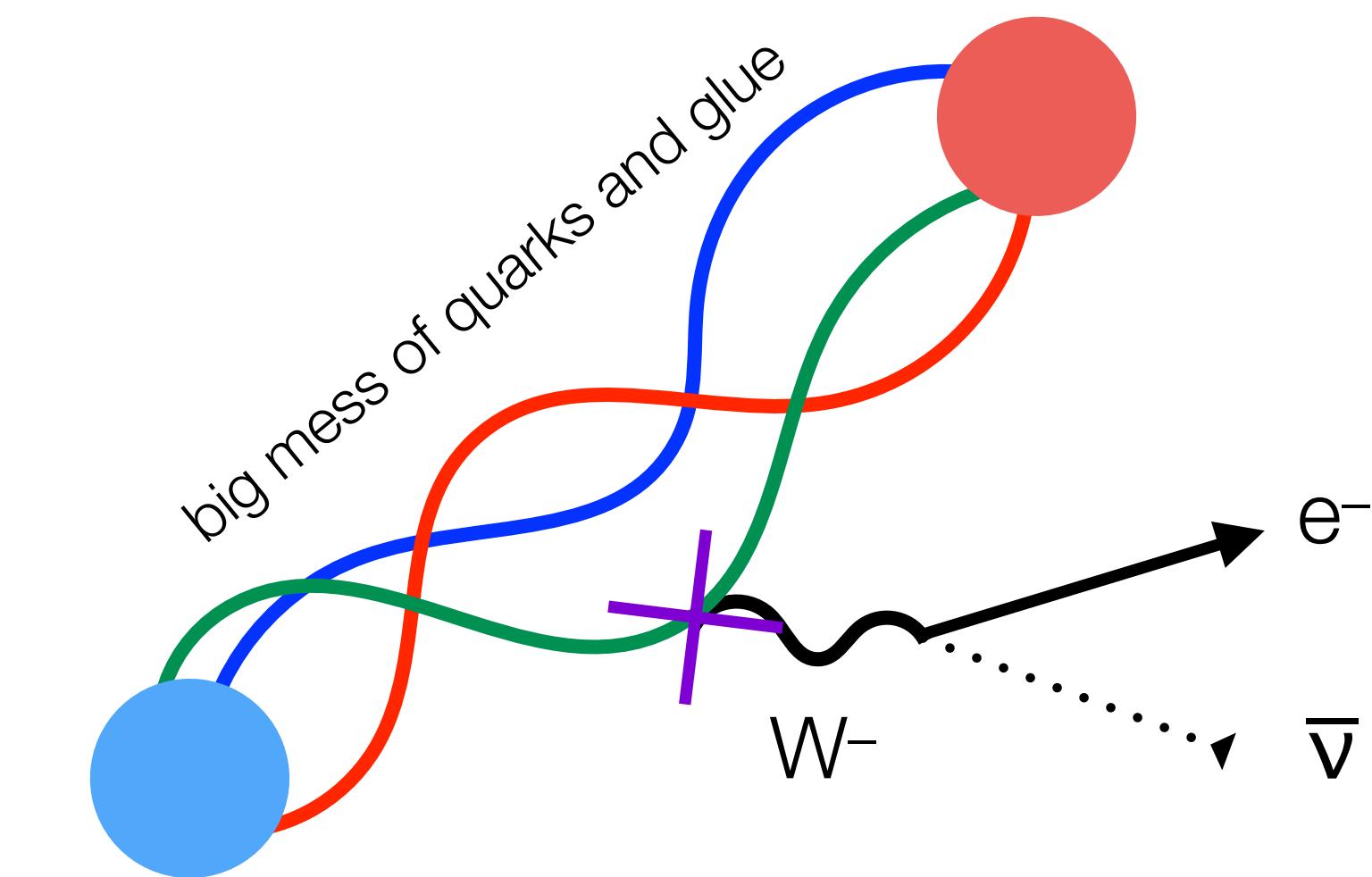
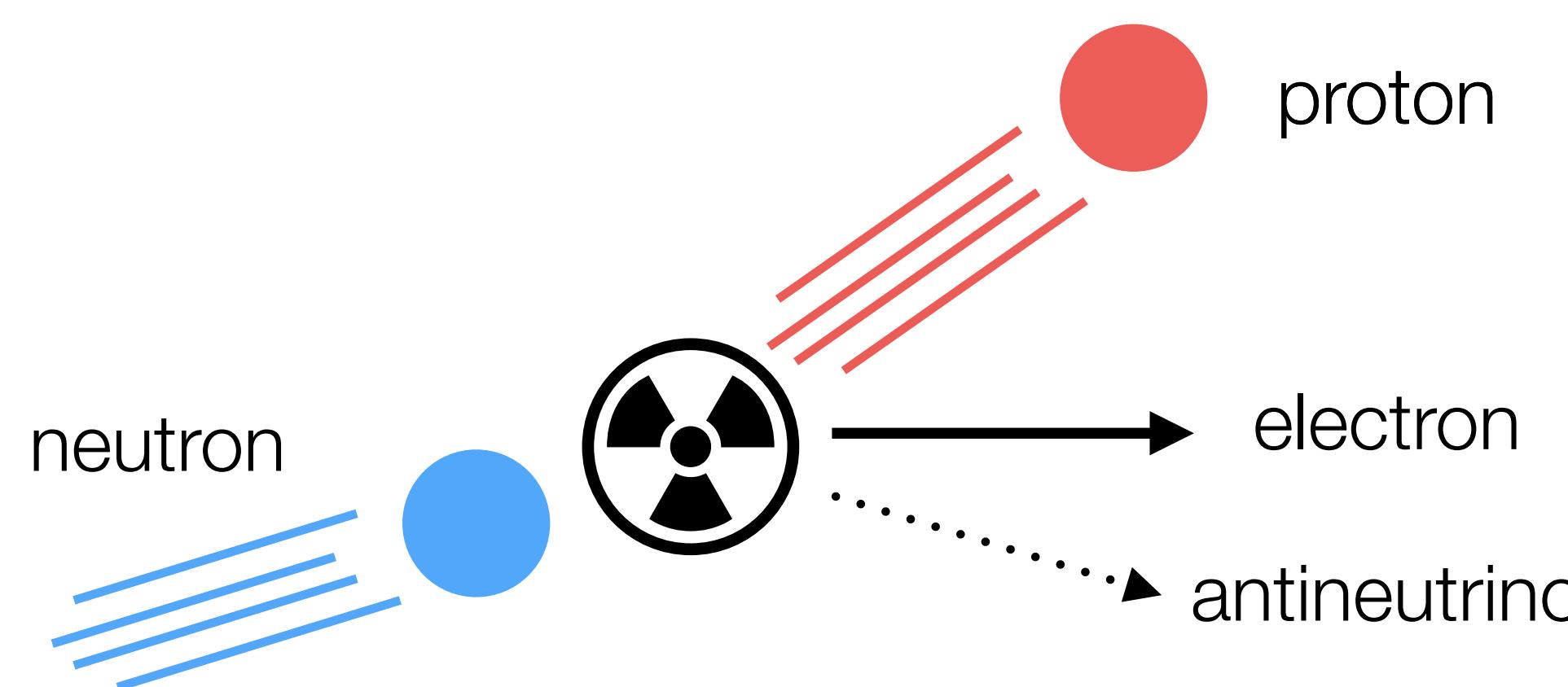


Chien-shiung Wu (1912-1997)
Smithsonian Institution

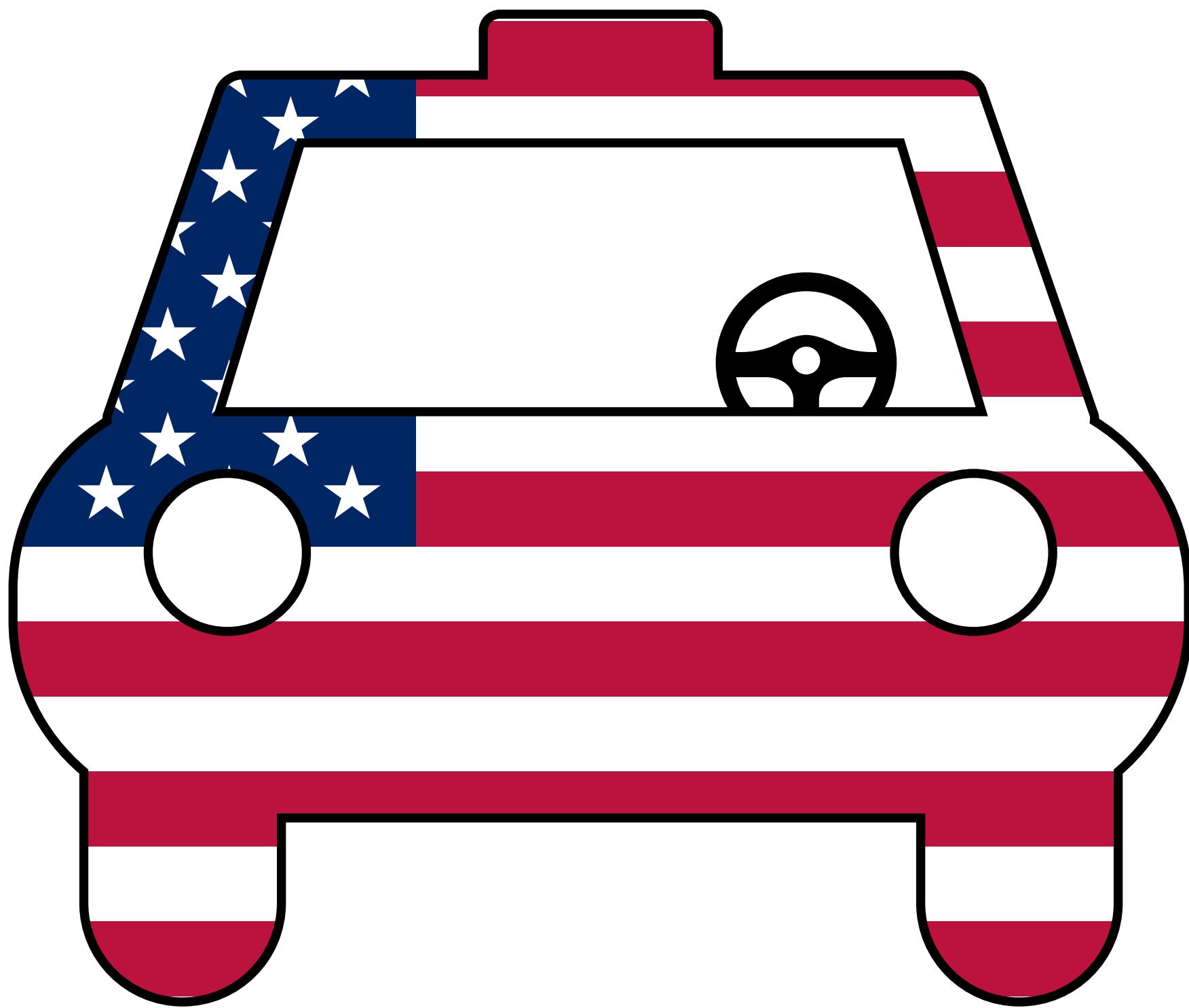
Left is alright

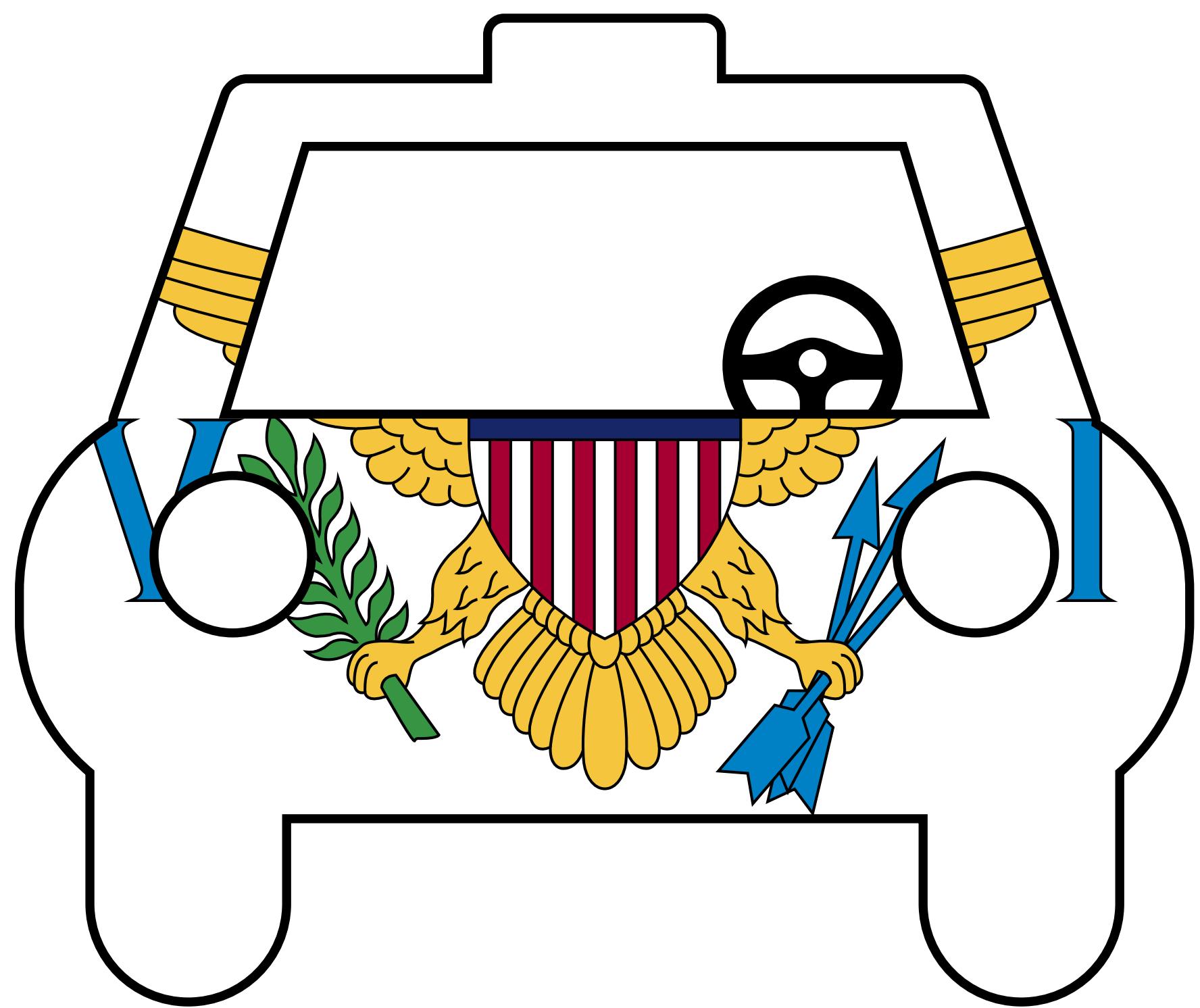
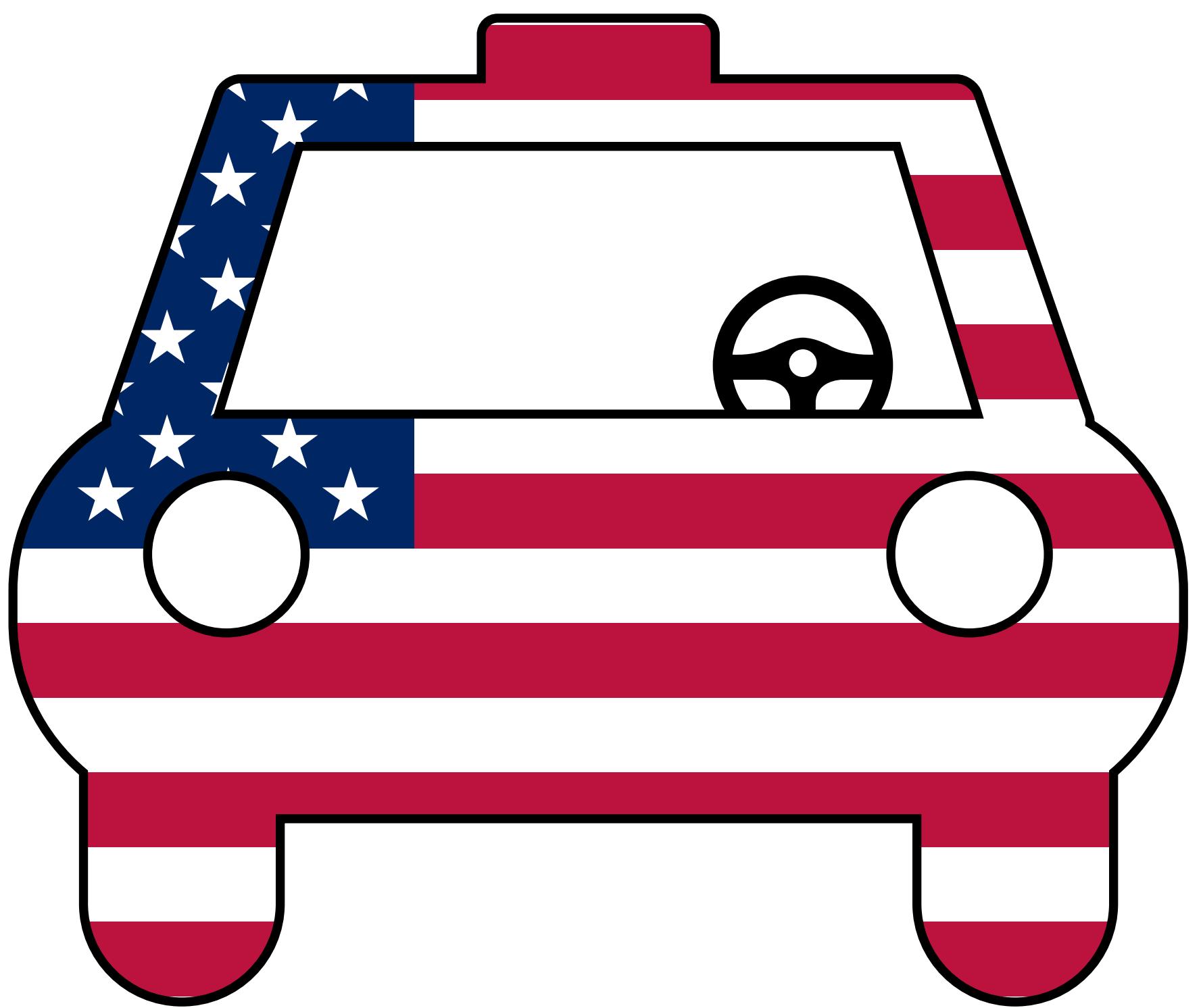


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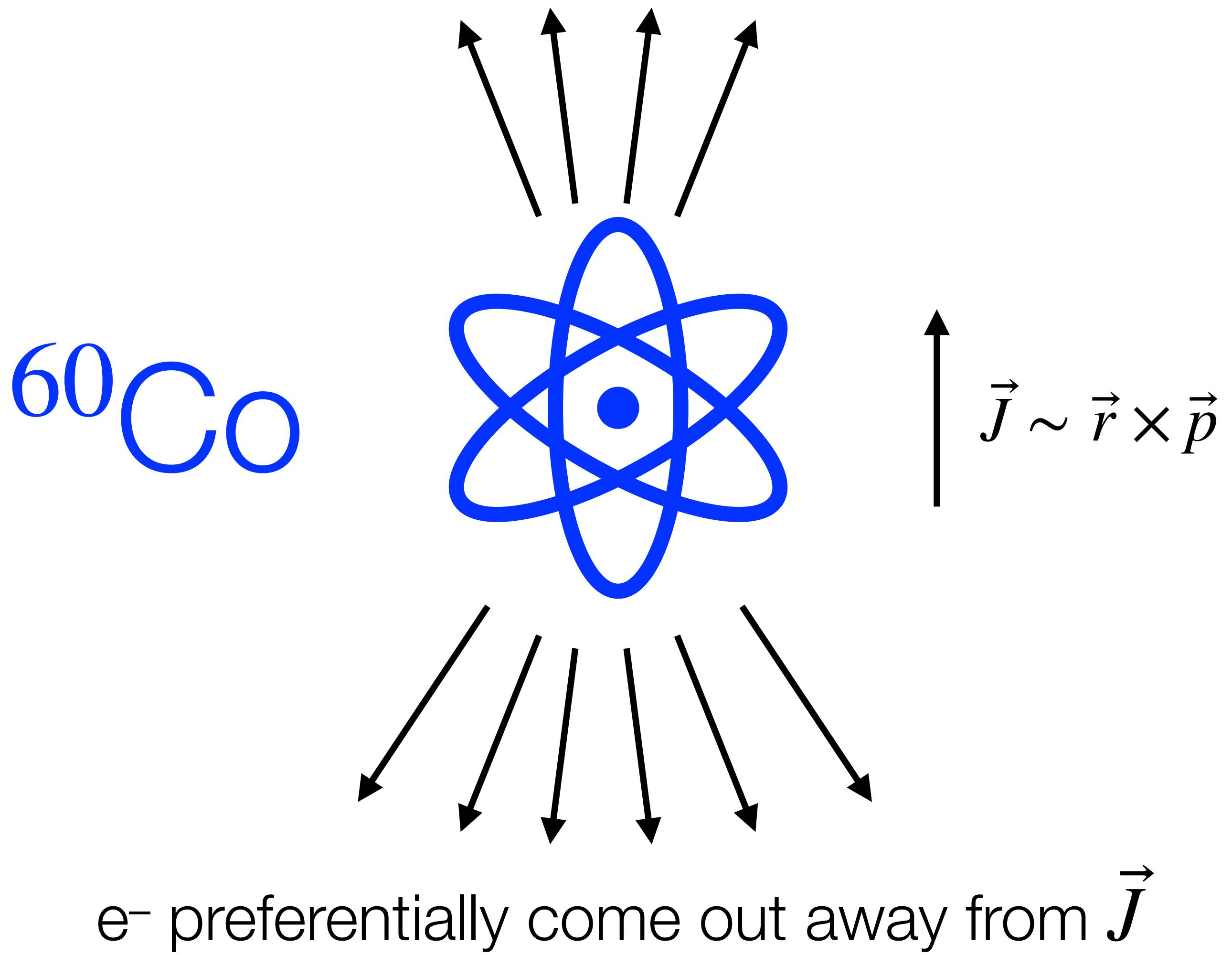


The weak force only talks to left-handed fermions!





Case study: Parity



Chien-shiung Wu (1912-1997)
Smithsonian Institution

"All the News
That's Fit to Print"

The New York Times.

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Telephone Lackawanna 4-1000

FIVE CENTS

LATE CITY EDITION

Condensation of U. S. Weather Bureau forecast:
Snow this morning, clearing in the
afternoon. Fair, cold tomorrow.

Temperature range today: 22-10.
Temperature range yesterday: 18-31.
Full U. S. Weather Bureau Report, Page 62.

PRESIDENT SEEKS 76 MILLION FUND TO FIGHT DROUGHT

Assures Wichita Conference
U. S. Will Have Other Plans
and Will Solve Problem

ENDS GREAT PLAINS TOUR

Strongly Backs Long-Range
Research With the Aim of
Resisting Dry Cycles

*Text of Eisenhower statement
is printed on Page 18.*

By DONALD JANSON
Special to The New York Times

WICHITA, Kan., Jan. 15.—President Eisenhower ended his tour of parched Great Plains states today with a pledge to seek \$76,000,000 in Federal funds for emergency drought relief.

The President also gave strong

Basic Concept in Physics Is Reported Upset in Tests

*Conservation of Parity Law in Nuclear
Theory Challenged by Scientists at
Columbia and Princeton Institute*

By HAROLD M. SCHMECK Jr.

Experiments shattering a fundamental concept of nuclear physics were reported yesterday by Columbia University.

The concept, called the "principle of conservation of parity,"

*The text of Columbia report
will be found on Page 24.*

has been accepted for thirty years. It must now be discarded, according to the Columbia scientists.

The principle of parity states that two sets of phenomena, one of which is an exact mirror of the other, behave in an identical fashion except for the mirror image effect.

The principle might be explained this way:

Assume that one motion picture camera is photographing a given set of actions and that another camera simultaneously

Continued on Page 24, Column 3

MACMILLAN GETS EISENHOWER WISH FOR ALL SUCCESS

Briton Responds With Equal
Warmth to Greetings on
His Appointment

By DREW MIDDLETON

Special to The New York Times

LONDON, Jan. 15—President Eisenhower has warmly congratulated Harold Macmillan on his appointment as Prime Minister, wishing him "every success" in his new post.

Mr. Macmillan, in his reply, has pledged his cooperation with the President in furthering friendship between the United States and Britain.

The exchange of letters was made public today by the Prime Minister's office. Mr. Macmillan also received similar messages of congratulation from Secretary of State Dulles and Secretary of the Treasury George M. Humphrey.

Regarded as Rebuttal



Associated Press Radiophoto

DELAYING ACTION IN EGYPT: Israeli soldiers setting up a road block yesterday between El Arish and Rafa during their withdrawal in the Sinai Peninsula. Yugoslav mem-

EGYPT TAKES OVER ASSETS OF BANKS OF BRITISH, FRENCH

Insurance Concerns Affected
Also by Nasser Regime's
'Egyptianization' Decrees

NATIVE OWNERSHIP AIM

Other Foreigners' Financial
Institutions Get 5 Years
Before Control Changes

By OSGOOD CARUTHERS
Special to The New York Times

CAIRO, Jan. 15—The Government announced today the "Egyptianization" of all British and French banks and insurance companies in Egypt.

All other foreign banks and insurance companies were given five years before they too would be "Egyptianized."

Under decrees to become effective tomorrow, the first anniversary of the promulgation of

The New York Times

Times Machine, Wednesday, January 16, 1957

THEORY IN PHYSICS IS REPORTED UPSET

Continued From Page 1

actly alike. The recent experiments indicate that this is not the case for some weak interactions of sub-atomic particles.

The idea that destroyed this principle originated with two theoretical physicists, Dr. Tsung Dao Lee of Columbia and Dr. Chen Ning Yang of the Institute for Advanced Study at Princeton, N. J. They suggested certain definitive experiments in papers on the subject: "Is Parity Conserved in Weak Interactions?"

The generally accepted belief, which had been a part of nuclear physics since 1925, was that parity should be conserved.

Two sets of experiments suggested by the two theorists showed that this parity was not conserved. A team of four Columbia physicists in collaboration with a member of the Institute for Advanced Study and a team at the National Bureau of Standards carried out the work.

The meeting that released the results of the experiments was held at 2 P. M. yesterday in Columbia's Pupin Physics Laboratories at 119th Street and Broadway. The chairman of the meeting was Dr. I. I. Rabi, Columbia's Nobel Prize-winning physicist.

"In a certain sense," Dr. Rabi commented on the development, "a rather complete theoretical structure has been shattered at the base and we are not sure how the pieces will be put together."

Physicists present at the meeting indicated that it might take a long time to evolve a new concept on the basis of the recently achieved results. One scientist said that nuclear physics, in a sense, had been battering for years at a closed door only to find that it is not a door at all but a likeness of a door painted on the wall. Now science is at least in a position to hunt for the true door again, he observed.

K Mesons Led to Doubts

The Columbia theorists were led to doubt the principle of parity because, during the last few years, phenomena had been described in high energy physics that could not be explained by existing theories. This was particularly true of the patterns by which certain sub-atomic particles called K mesons decayed. Nobody was able to formulate a theory to account for both of the two methods of decay that they followed.

Dr. Lee and Dr. Yang suggested that perhaps it would be necessary to give up the principle of parity to gain an explanation of the sub-atomic interactions. They found that certain experiments dealing with particles better known than the K mesons could resolve the puzzle.

One set of experiments, done in a low temperature physics laboratory of the Bureau of Standards, showed that disintegrating nuclei of radioactive

Text of Columbia Report on Physics Experiments

The Meaning of Parity (Mirror Symmetry)

I. Introduction

The Department of Physics of Columbia University announces a development of very profound importance uncovered in very recent experiments in the subject of the physics of elementary particles. These experiments are:

(1) The beta-decay of oriented nuclei—Prof. C. S. Wu

of Columbia University in collaboration with Ernest Ambler, R. W. Hayward, D. D. Hoppes and R. P. Hudson of the National Bureau of Standards.

(2) The angular asymmetry

in electron decay of mu mesons—Dr. Richard L. Garwin, Prof. Leon M. Lederman and Mr. Marcel Weinrich of Columbia University. (Note: Dr. Garwin is also a senior staff member of the I. B. M. [International Business Machines] Watson Scientific Laboratory at Columbia.)

II. Significance

Both of the above experiments (described in more detail below) were suggested by two theoretical physicists, Prof. T. D. Lee of Columbia University and Prof. C. N. Yang of the Institute for Advanced Study, Princeton, N. J.

The first of a series of three papers on the subject was entitled "Is Parity Conserved in Weak Interactions?" The experiments designed to answer this question give a decisive answer—parity is not conserved—thus destroying one of the basic laws built into all physical theories of the past thirty years.

Parity

The concept of parity, although actually significant only in the realm of microscopic (atoms and particles) physics, has a well defined everyday definition. One way of describing this is as follows:

Suppose we are in communication with an intelligent civilization on another world and wish to determine whether their clocks run in the same sense as ours do—or again whether they mean the same thing by left-handed and right-handed as we do. We have always believed that communication of this idea, in the spirit of this analogy, is impossible. There was no absolute, universal sense to "Handedness." However, the stranger's laws of physics are perfectly good—even if his definition is opposite to ours for, say, a left-hand screw and a right-hand screw.

The statement that the two worlds, one based upon a left-handed system and one based upon a right-handed system, have the same laws in physics is known as an "invariance principle," i. e., the laws of physics are said to be invariant or unchanged, if the

ingoing particle with a spinning bullet. If the shape of the bullet were a perfect cylinder, there would be no screw defined, or no "handedness," since the two ends of the bullet are identical.

The new concept of particles is now in analogy with a normal bullet (pointed nose) which differentiates one end of the spin from the other. Particles which "point" in one direction relative to the sense of rotation are called right-handed, etc. The fact that such particles exist on this world and on the other world now permits an absolute identification of right and left.

way to a correct and unifying theory of elementary particles. Lee and Yang also point out that the overall symmetry of the universe may still be preserved by assuming that, if our galaxy is essentially right-handed, some distant galaxy may be in turn left-handed. It may be that this assumed distant galaxy is identical to the hypothetical anti-matter, now a subject of intense speculation. This would represent an enormous simplification in our theoretical attack on the structure of the universe.

III. Theoretical Background

The proposal that the parity law may not be true was made by Lee and Yang last summer. This was in an attempt to reconcile data obtained with the super-atom smasher, the Brookhaven Cosmotron and the Berkeley Be-

vatron. The data consisted of the study of the properties of the unstable Kmesons, particles which were only recently discovered (1952-53). One aspect of Kmeson disintegration seemed to violate the parity law. So deeply rooted was this law, that the entire world of physics was completely baffled by the K-meson puzzle, the general feeling being that the Kmesons, being newly discovered, were just not well enough understood. Lee and Yang boldly made the break and, in their now historic paper, they re-examined the consequences of removing the parity law for radioactive disintegrations of nuclei and particles. They found, to their surprise, that none of the existing data would be in contradiction and that certain crucial experiments, dealing with more well-known particles, would give decisive answers.

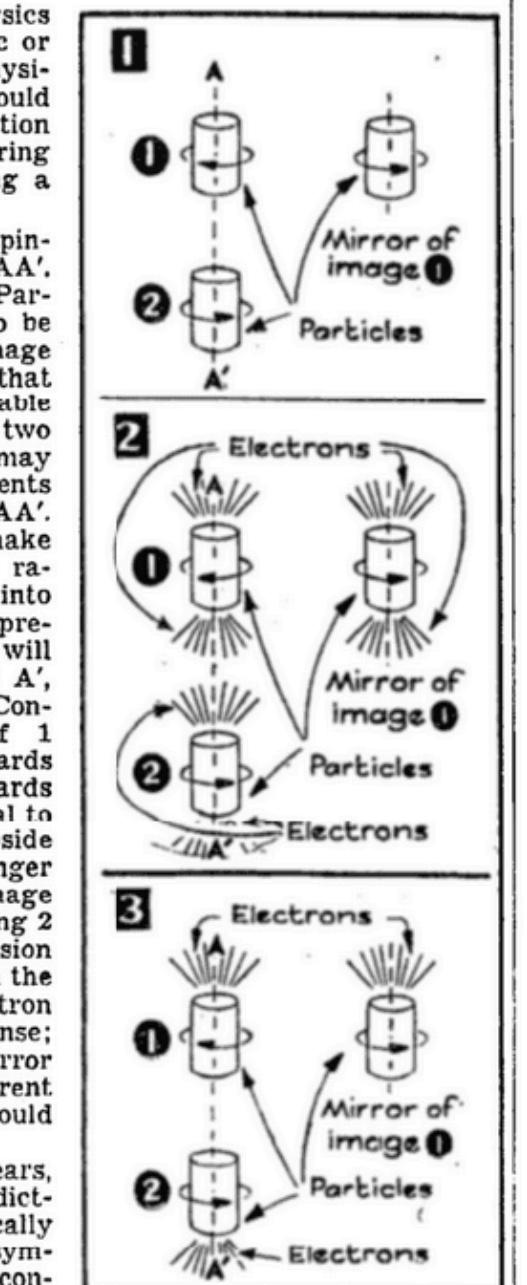
IV. The Experiment Oriented Nuclei

To detect the "handedness" of particles, the radioactive nucleus Cobalt 60 was cooled to a temperature of 0.01° above absolute zero [−273.1 Centigrade]. At this temperature, all thermal motions are reduced to extremely small values. The application of a magnetic field will cause most of the cobalt nuclei, which are known to be spinning, to align themselves, like small magnets, parallel to the applied magnetic field. The radioactive cobalt nuclei disintegrate, giving off electrons. The crucial point is the comparison of the number of electrons emitted along the direction of spin to the number going in the opposite direction.

The very fact that these numbers are different indicates the favoring of a direction associated with the spin, that is, a "handedness" in the sense of a screw. Moreover, the magnitude of the difference was sufficiently large to indicate a violation of charge conjugation invariance.

The technical aspects were quite difficult. At the request of and in collaboration with Professor Wu, the National Bureau of Standards Low Temperature Physics Group undertook experiments to verify the theoretical considerations. This group assisted by National Bureau of Standards specialists in radioactive measurements provided the techniques and experience for completing the project successfully. Scintillation counters had to be installed within the complex vacuum and cooling system and extreme care had to be taken to eliminate spurious effects. This work was partially supported by the Atomic Energy Commission.

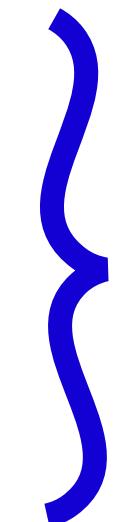
Meson Decays
In this experiment two parity violations were detected as



Marcel Weinrich, graduate research assistant, Columbia University.

Symmetries of the Standard Model

- Time invariance
- Rotational invariance
- Translational invariance
- ~~Parity~~
- C: Charge conjugation
- T: Time reversal
- $SU(3) \times SU(2) \times U(1)$
- Baryon, Lepton number conservation

 spacetime symmetries
 discrete symmetries?

gauge symmetry
accidental symmetries?

	mass \rightarrow	charge \rightarrow	spin \rightarrow	
QUARKS				
u	$\approx 2.3 \text{ MeV}/c^2$	2/3	1/2	up
c	$\approx 1.275 \text{ GeV}/c^2$	2/3	1/2	charm
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g	0	0	1	gluon
H	$\approx 126 \text{ GeV}/c^2$	0	0	Higgs boson
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b	$\approx 4.18 \text{ GeV}/c^2$	-1/3	1/2	bottom
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W	80.4 GeV/c^2	± 1	1	W boson
GAUGE BOSONS				

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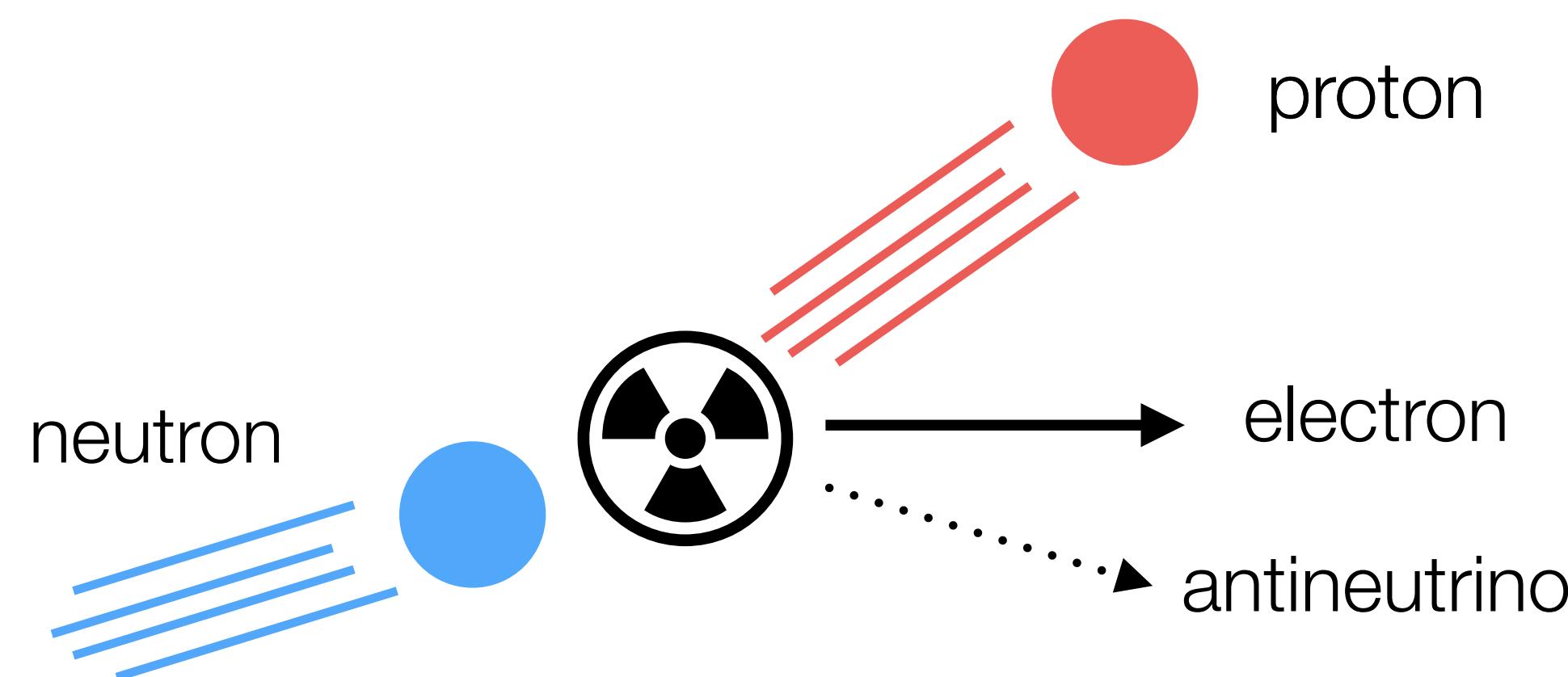
Mysterious Mesons

	Electromagnetism	Weak	Strong
C Charge	✓	✗	✓
P Parity	✓	✗ θ - τ	✓
T Time Reversal	✓	✗ $K\bar{K}$	✓
L Lepton number	✓	✓	
B Baryon number	✓	✓	✓

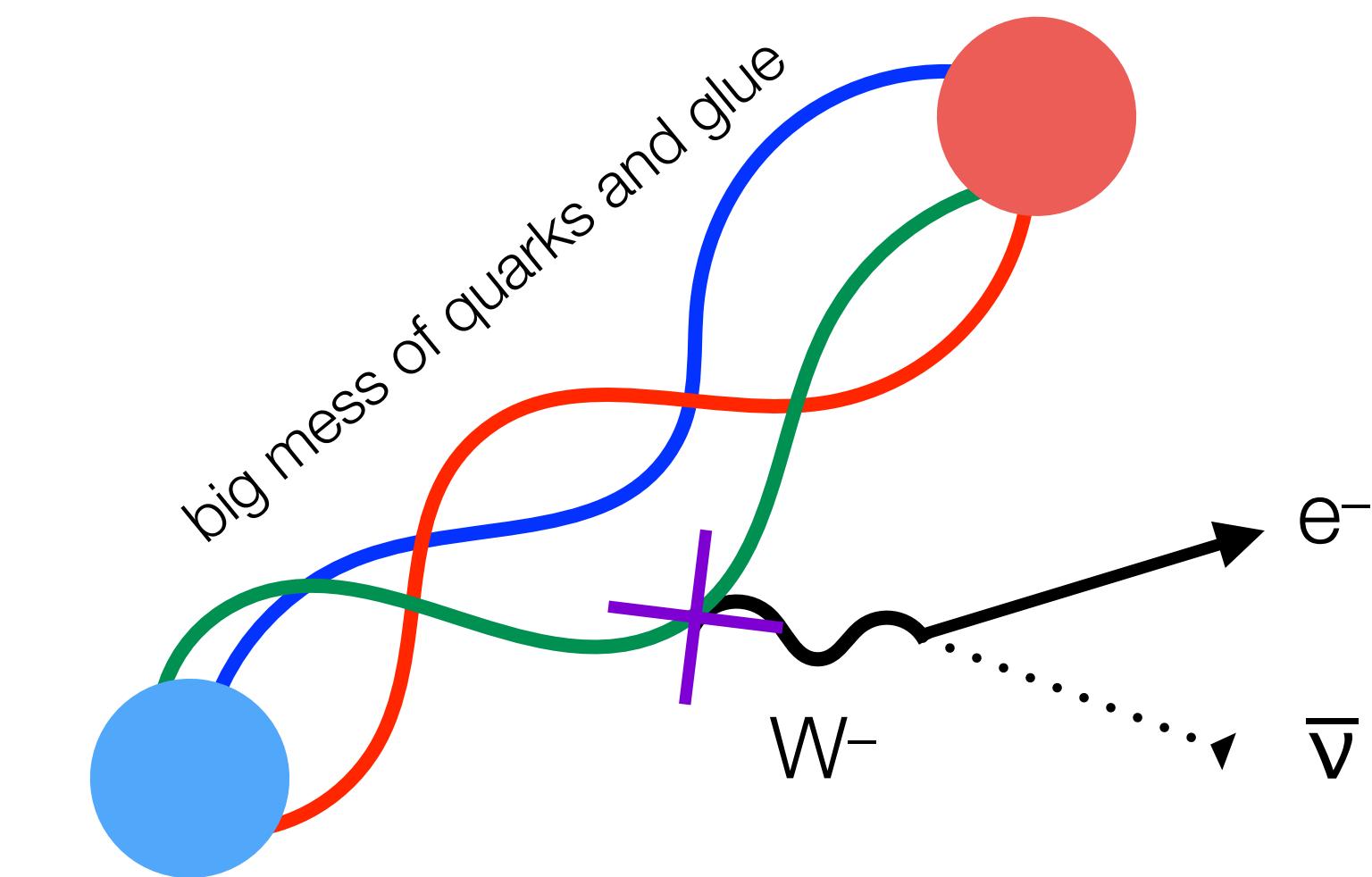
Left is alright



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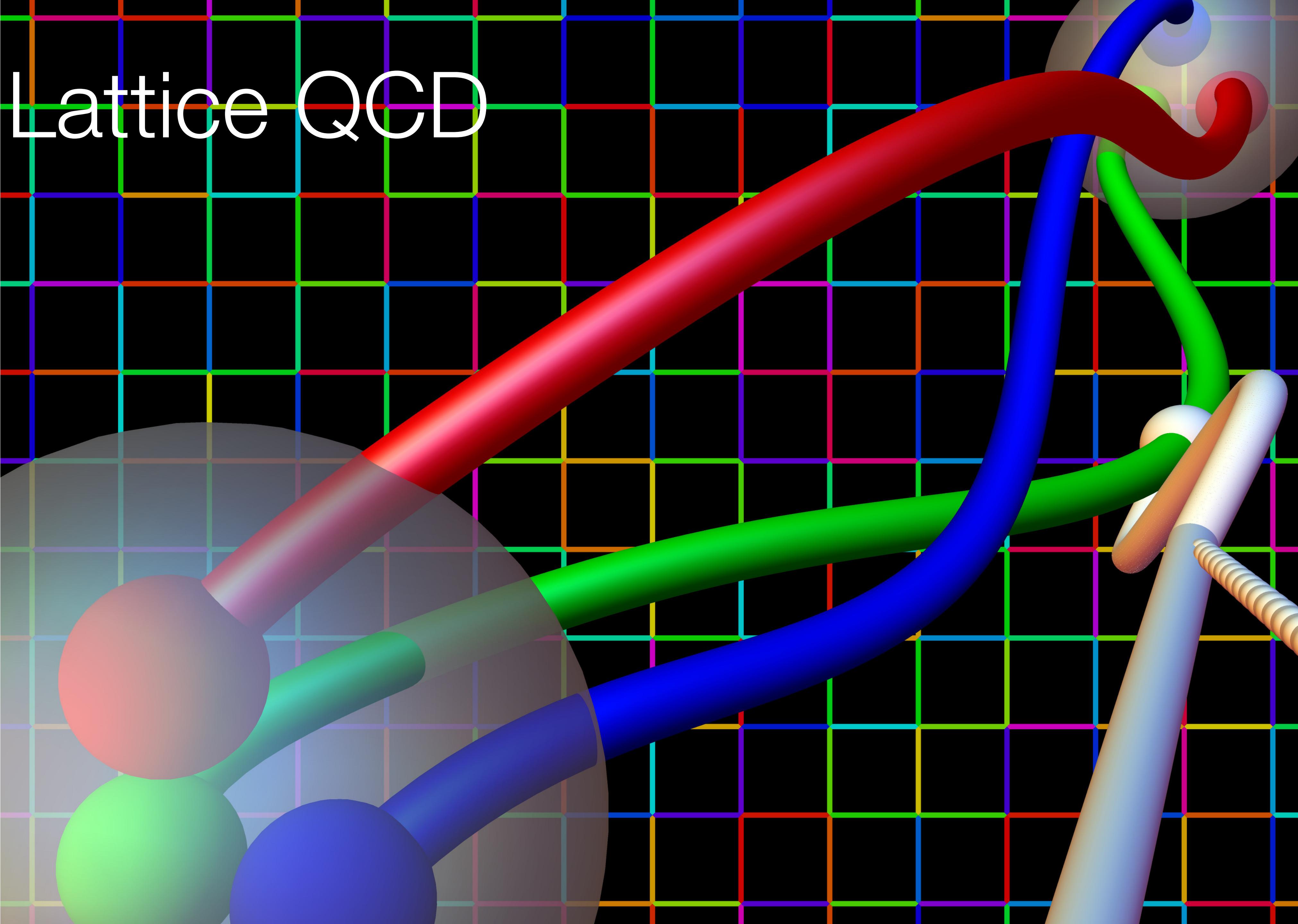


Measure g_A experimentally

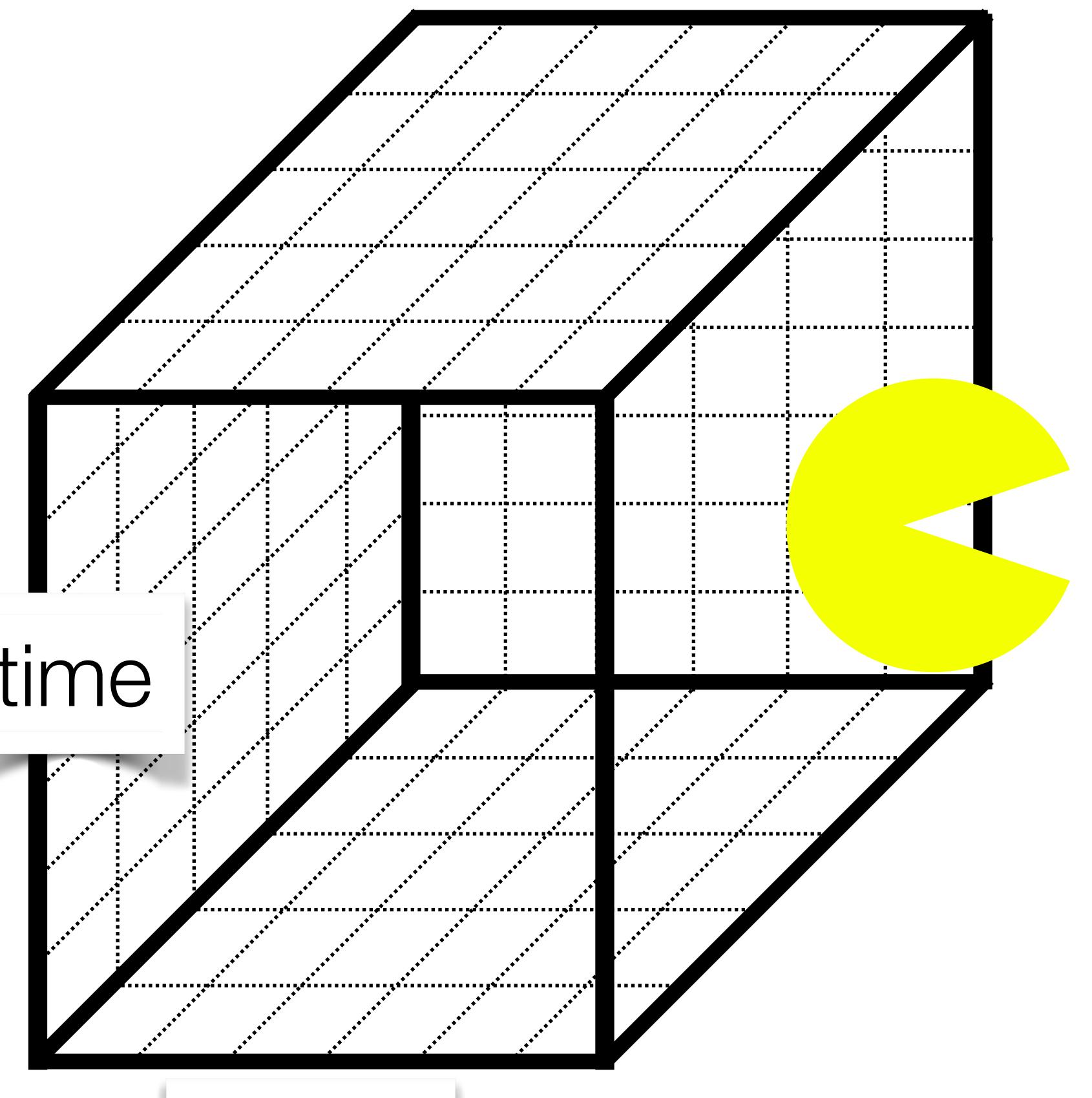


Compute g_A from the SM

Lattice QCD



Lattice QCD



$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}F^2 + \bar{\psi}(iD + m)\psi$$

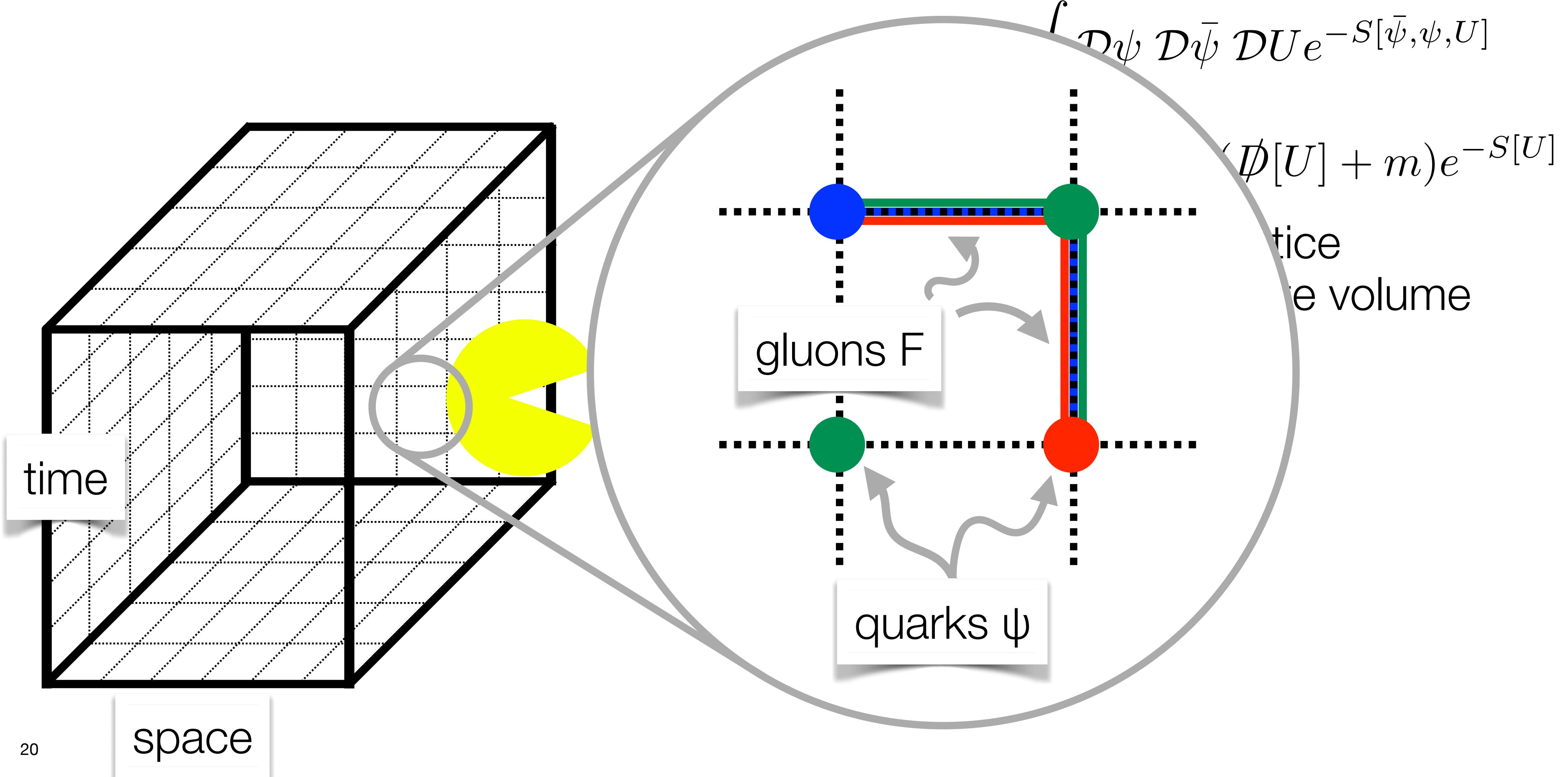
$$\mathcal{Z} = \int \mathcal{D}\psi \mathcal{D}\bar{\psi} \mathcal{D}U e^{-S[\bar{\psi}, \psi, U]}$$

$$= \int \mathcal{D}U \det(D[U] + m) e^{-S[U]}$$

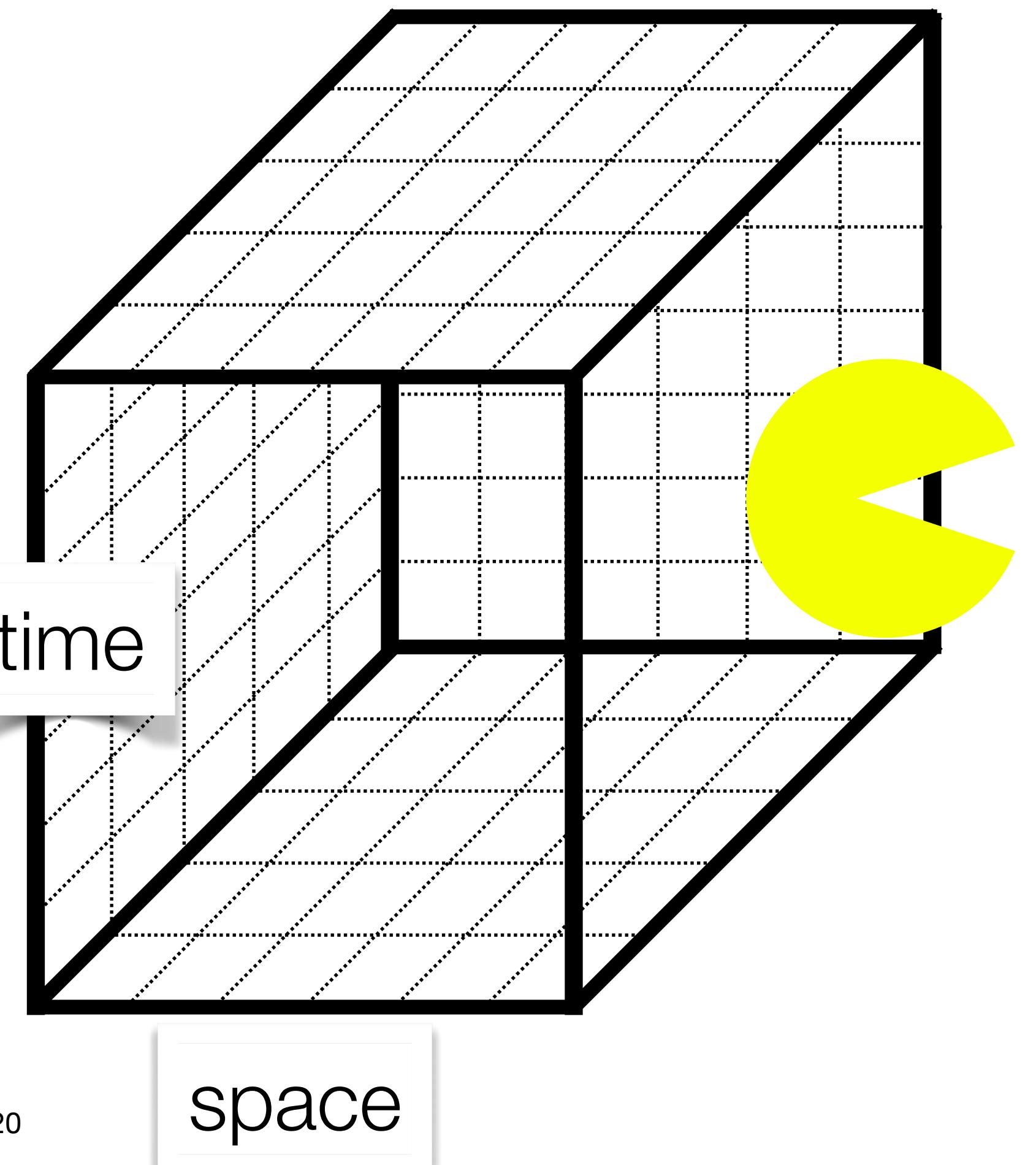
lattice
finite volume

Lattice QCD

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}F^2 + \bar{\psi}(i\cancel{D} + m)\psi$$



Lattice QCD



$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4}F^2 + \bar{\psi}(i\cancel{D} + m)\psi$$

$$\begin{aligned}\mathcal{Z} &= \int \mathcal{D}\psi \mathcal{D}\bar{\psi} \mathcal{D}U e^{-S[\bar{\psi}, \psi, U]} \\ &= \int \mathcal{D}U \det(\cancel{D}[U] + m) e^{-S[U]}\end{aligned}$$

Probability

$$\{U_1, U_2, U_3, \dots, U_N\}$$

Markov Chain Monte Carlo

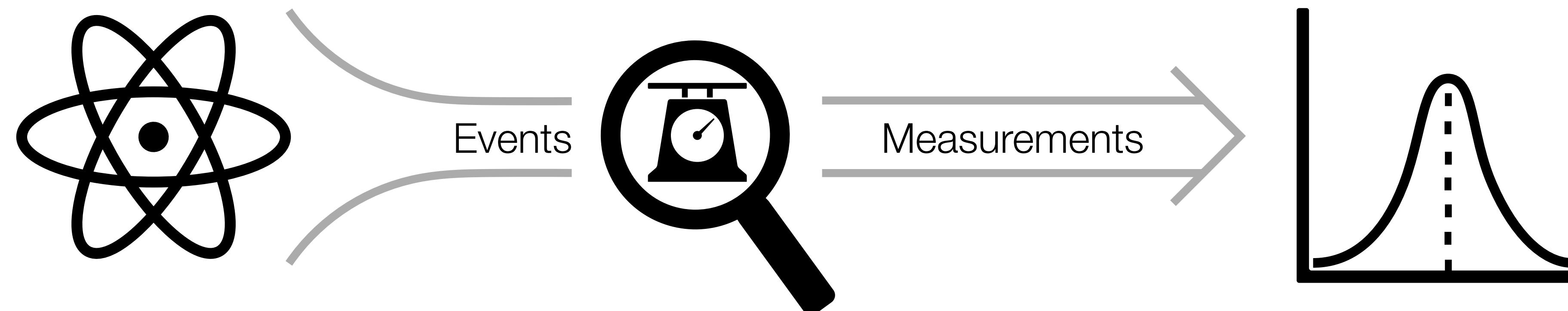
$$\langle \mathcal{O} \rangle = \frac{1}{\mathcal{Z}} \int d\mathcal{Z} \mathcal{O}[U]$$

$$\approx \frac{1}{N} \sum_{i=1}^N \mathcal{O}[U_i]$$

with uncertainties scaling like $\frac{1}{\sqrt{N}}$

Analogy with Experiment

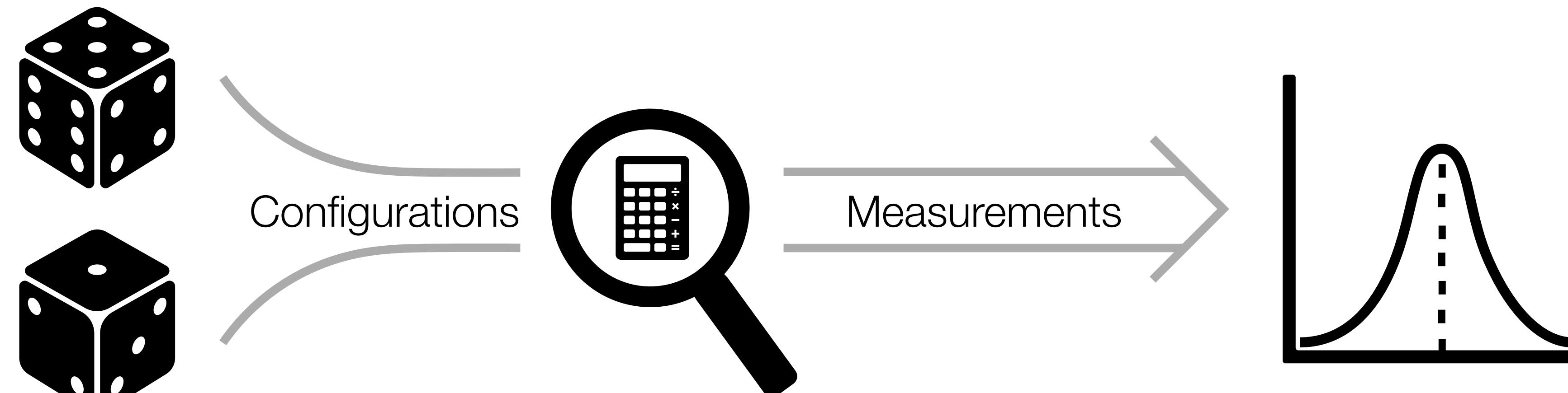
- ✓ Statistical errors are improved with run time (budget)
- ✓ Systematic errors are understood + controlled



Nature

Detector

Analysis

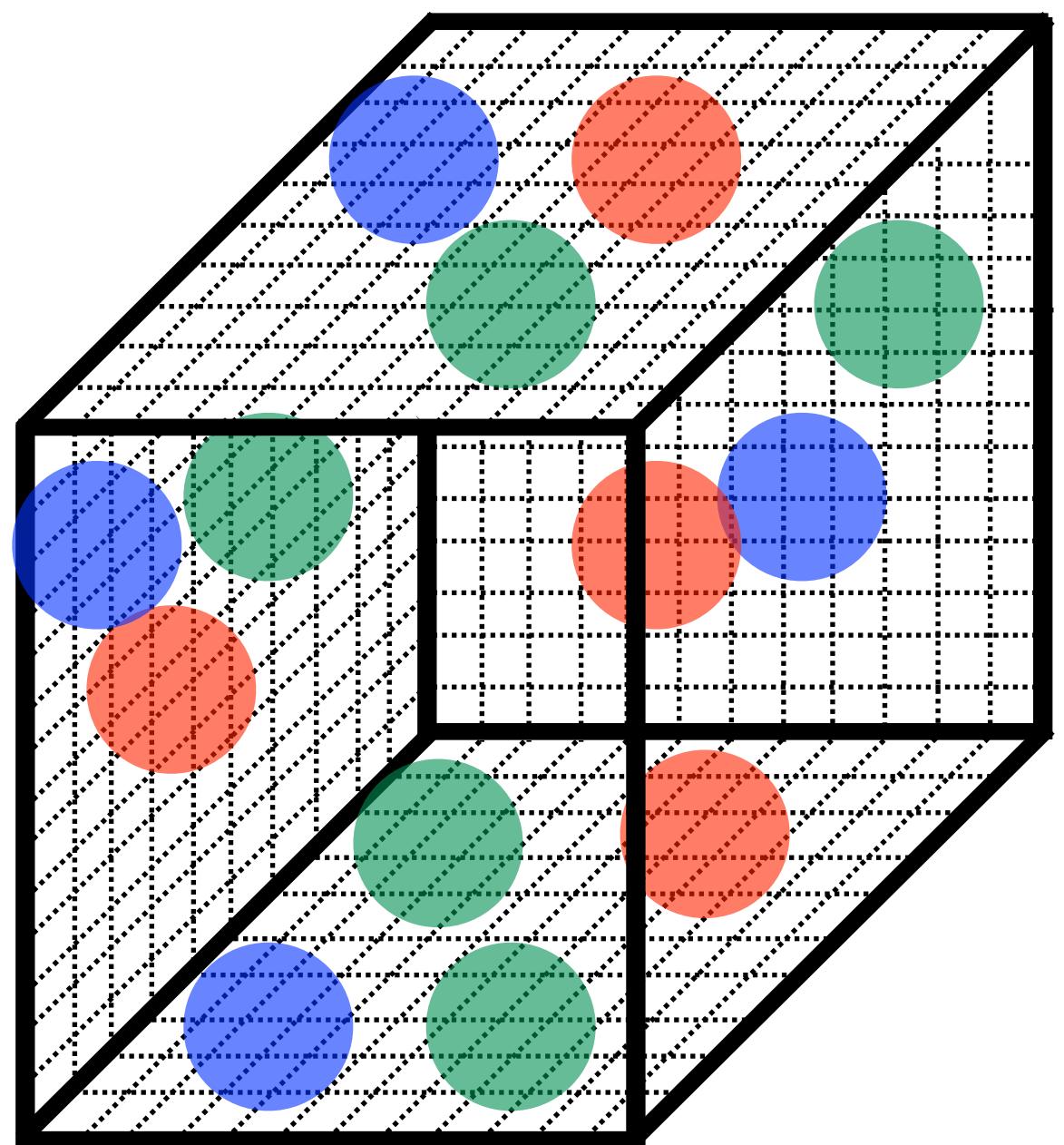


Monte Carlo

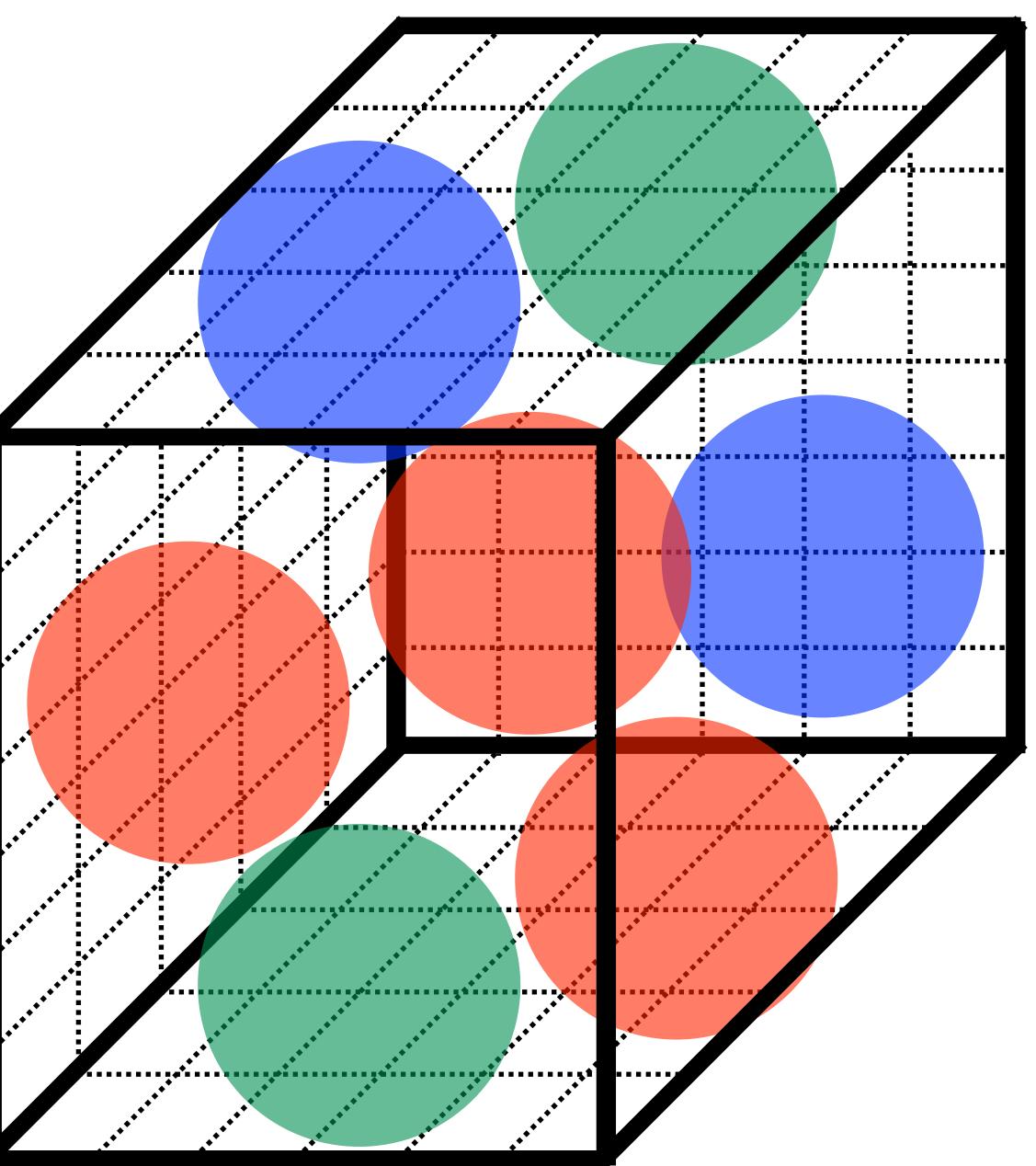
Observable

Analysis

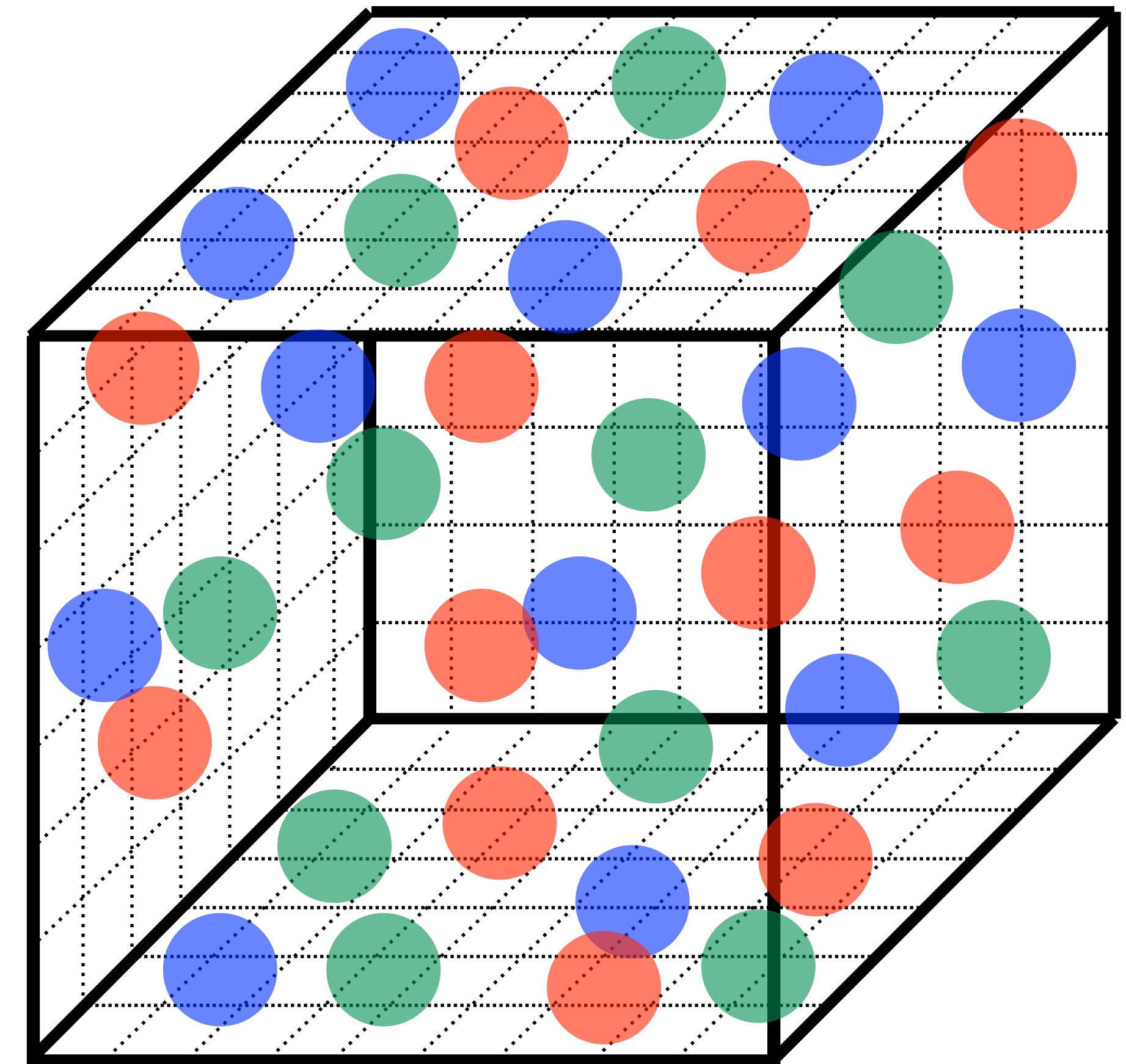
LQCD Systematics



continuum limit



physical quark masses



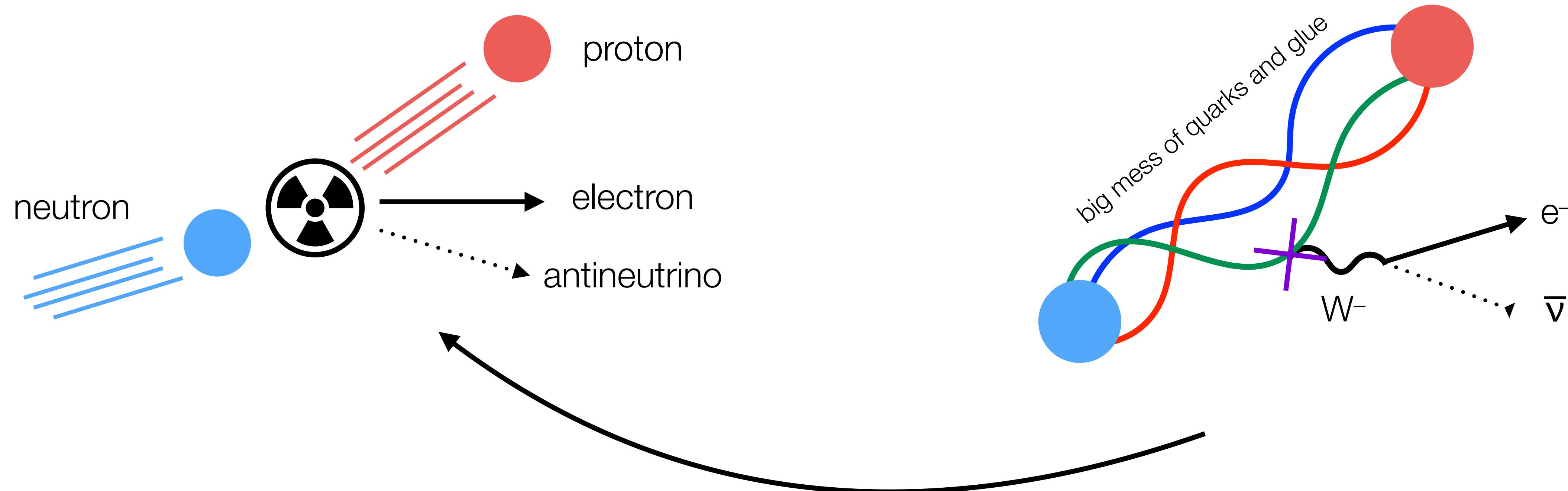
infinite volume limit



High performance computing to the rescue!



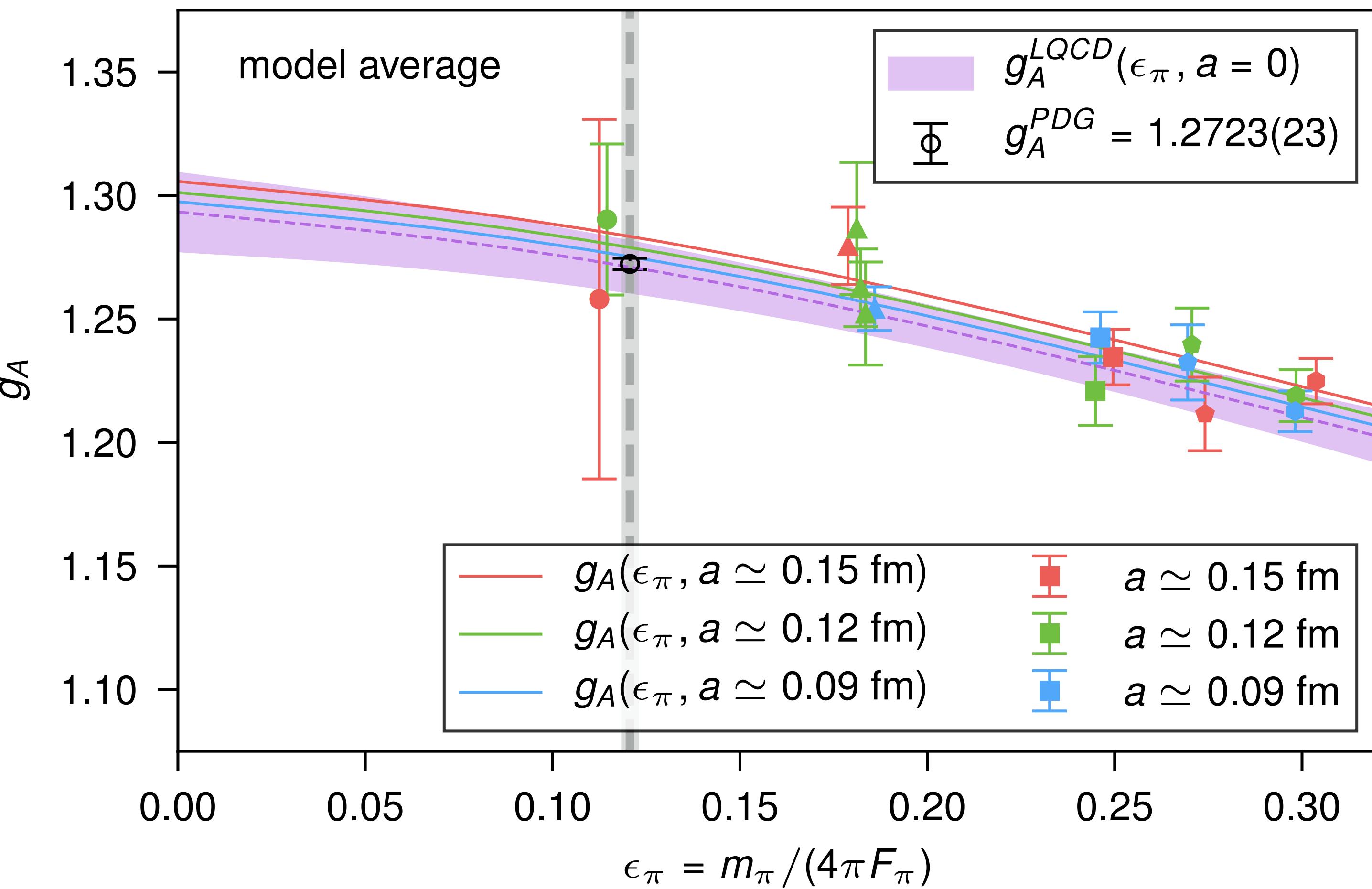
How do the weak interactions trickle up?



Use the Standard Model to *predict* the nucleon axial coupling g_A
so measurements can tell us if there's something more.

$g_A^{\text{QCD}} = 1.271(13)$

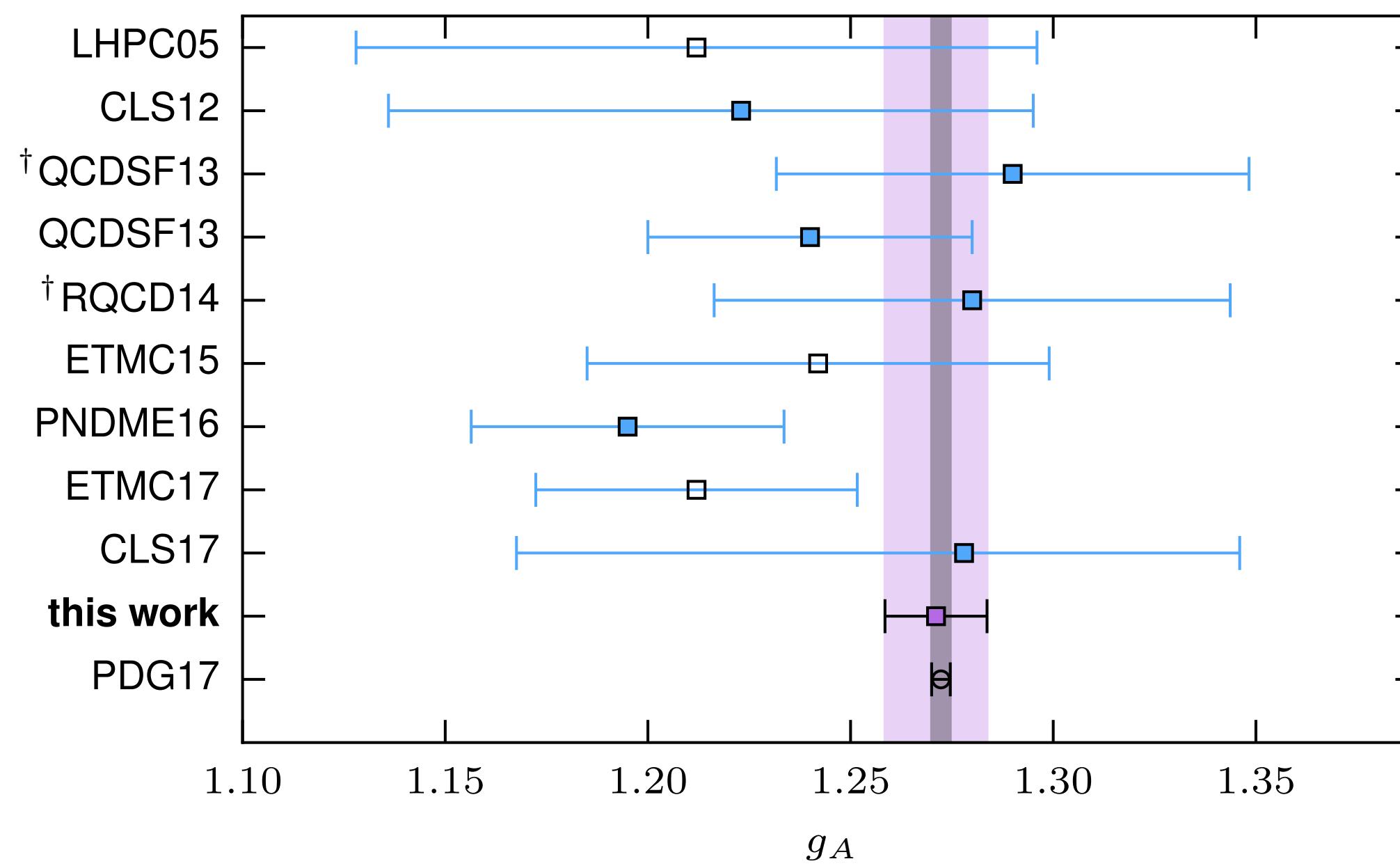
Nature 558:91–94, 2018 arXiv:1805.12130



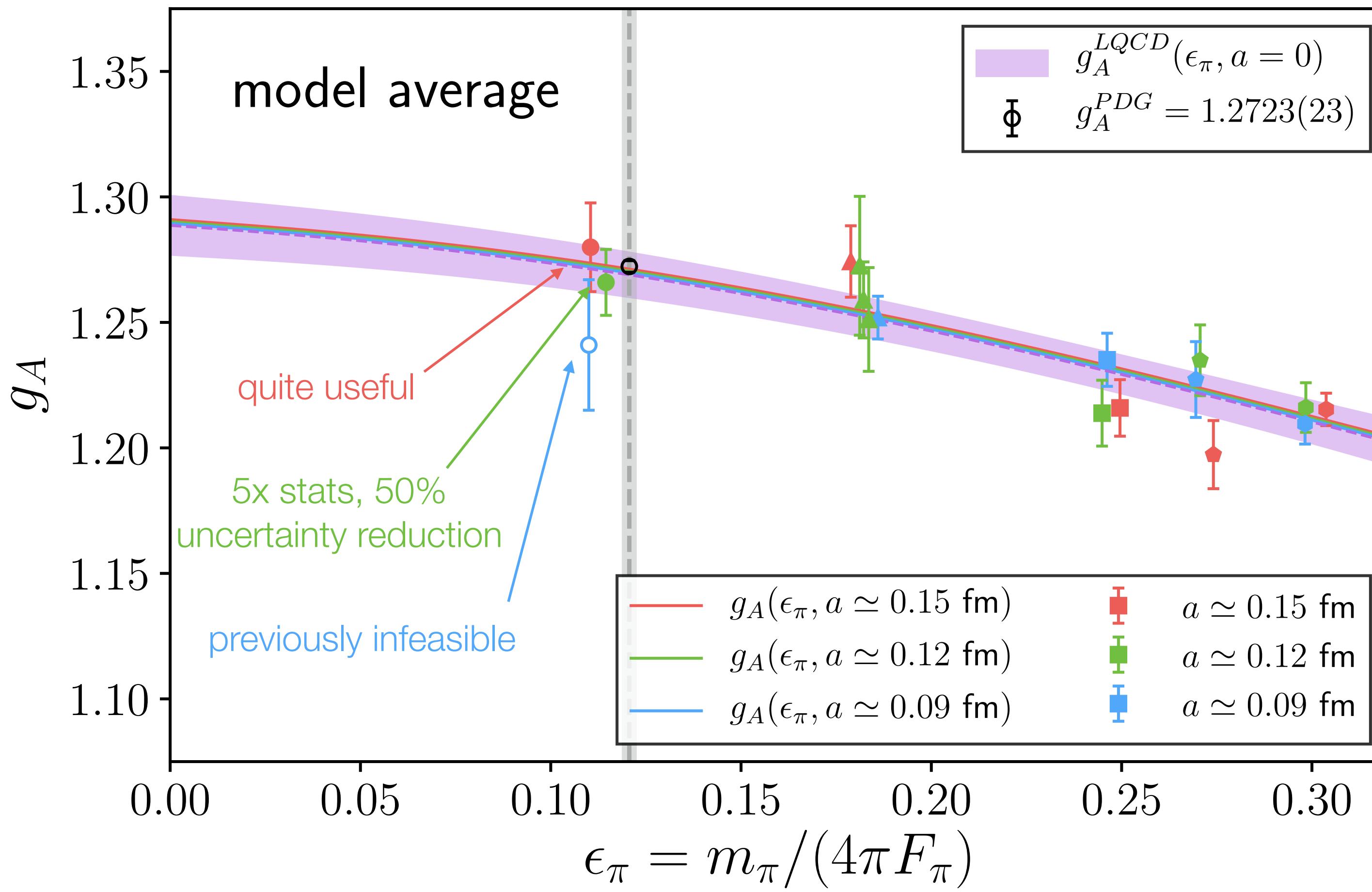
A per-cent-level determination of the nucleon axial coupling from quantum chromodynamics

C. C. Chang^{1,2}, A. N. Nicholson^{1,3,4}, E. Rinaldi^{1,5,6}, E. Berkowitz^{6,7}, N. Garron⁸, D. A. Brantley^{1,6,9}, H. Monge-Camacho^{1,9}, C. J. Monahan^{10,11}, C. Bouchard^{9,12}, M. A. Clark¹³, B. Joó¹⁴, T. Kurth^{1,15}, K. Orginos^{9,16}, P. Vranas^{1,6} & A. Walker-Loud^{1,6*}

- New methods
- Performant code
- Cutting-edge supercomputers



Better, faster, stronger

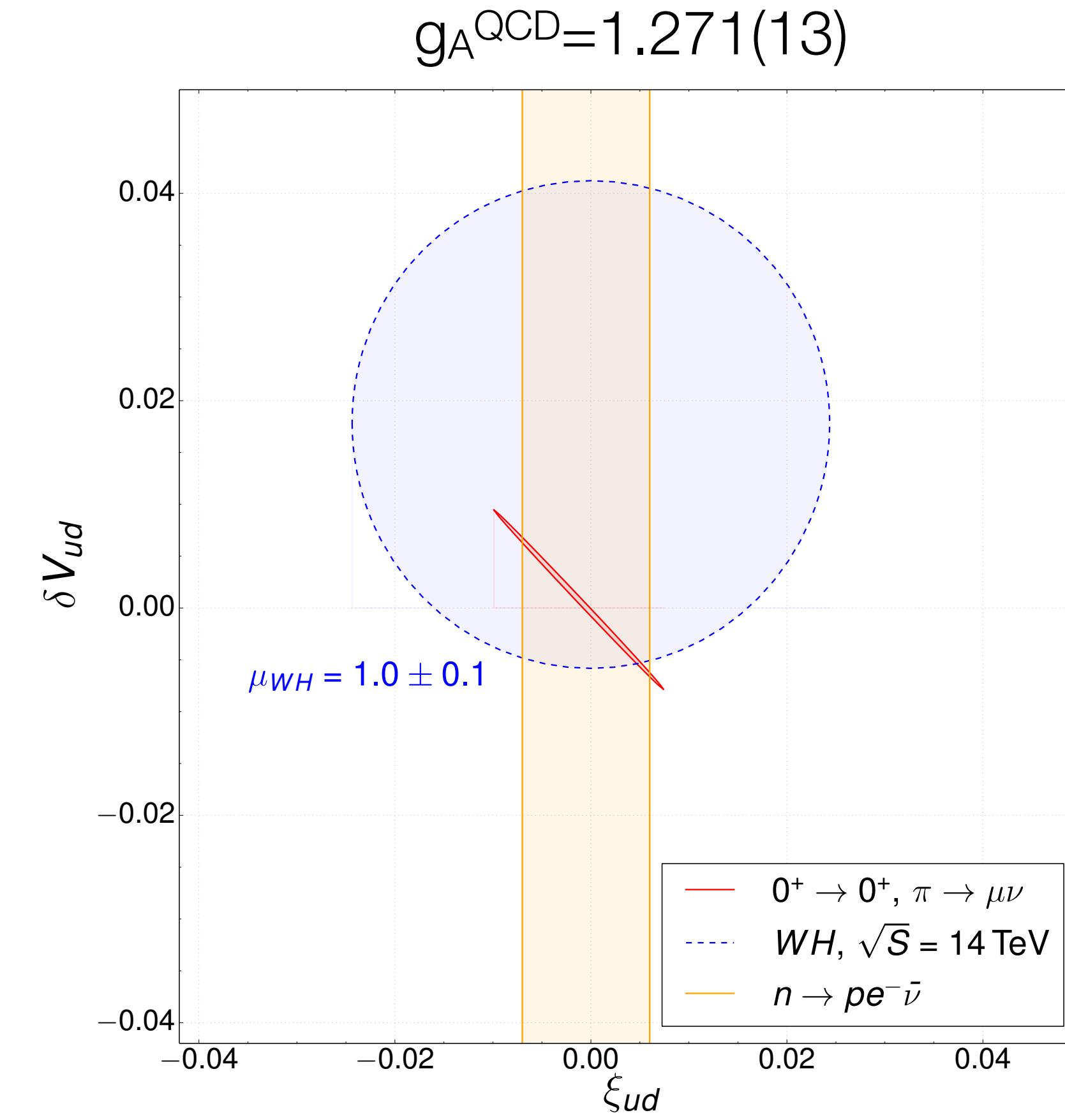
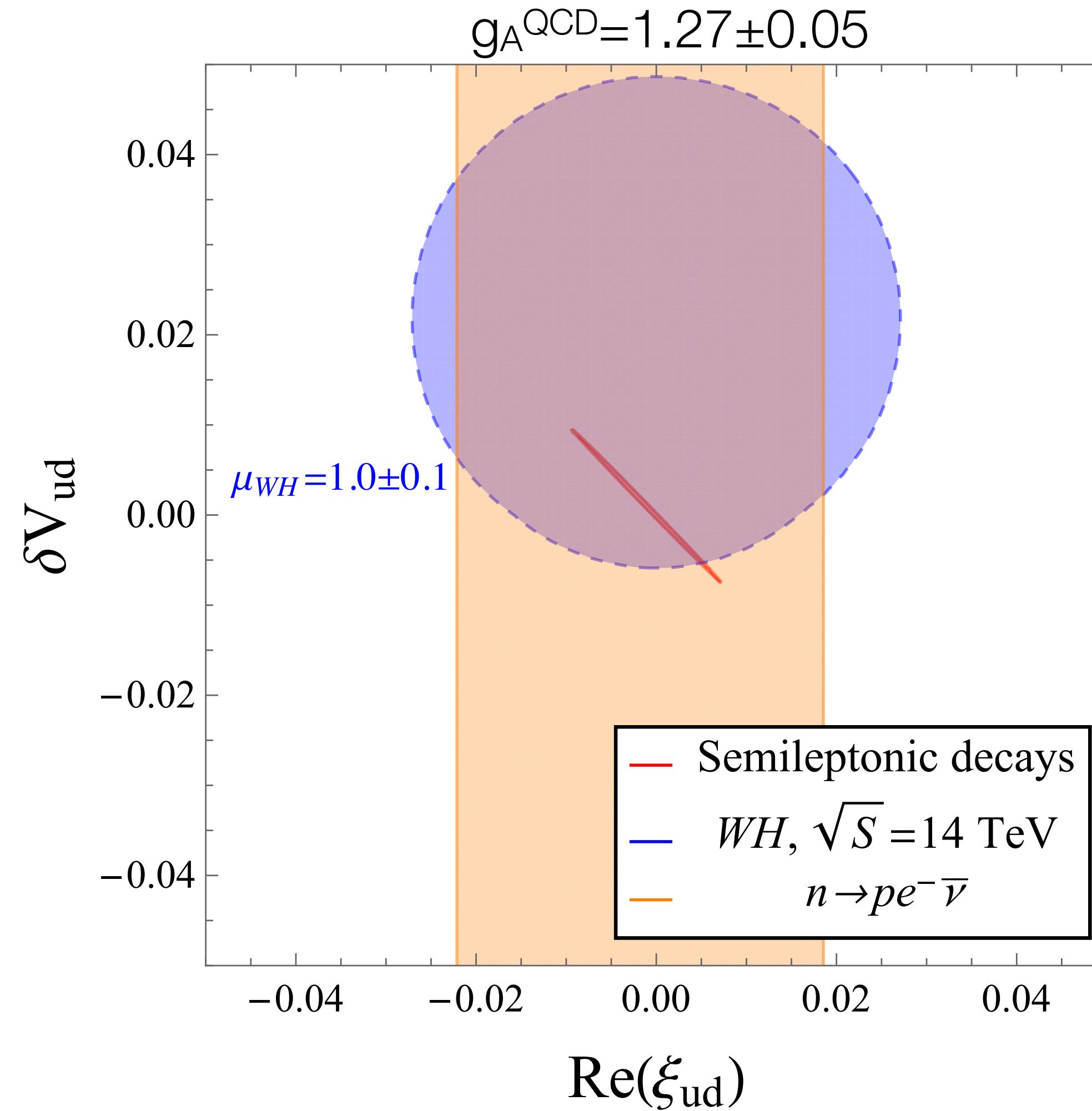


- In 2.5 weekends on Sierra we accomplished more than 5 times as much as a year on Titan
- New machines are **disruptively faster**.
- The golden age of lattice QCD is just around the corner here!



The hunt for new physics

Alioli, Cirigliano, Dekens, de Vries, Mereghetti JHEP 1705 (2017) 086 arXiv:1703.04751



New CKM-like physics

New right-handed currents

Fundamental Symmetries

	Electromagnetism	Weak	Strong
C Charge	✓	✗	✓
P Parity	✓	✗ θ - τ	✓
T Time Reversal	✓	✗ $K\bar{K}$	✓
L Lepton number	✓	✓	
B Baryon number	✓	✓	✓

EFTs + Fundamental Symmetry

The Standard Model

- A quantum field theory with particular symmetries.
- No gravity, **neutrino masses + oscillations, dark matter**
- Otherwise, the ultimate description of every physical phenomenon **thus far observed!**

Baryon number is conserved.

QUARKS	mass \rightarrow	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$	GAUGE BOSONS
	charge \rightarrow	2/3	2/3	2/3	0	0	
	spin \rightarrow	1/2	1/2	1/2	1	0	
u							gluon
c							Higgs boson
t							
d	$\approx 4.8 \text{ MeV}/c^2$	-1/3					photon
s	$\approx 95 \text{ MeV}/c^2$	-1/3					
b	$\approx 4.18 \text{ GeV}/c^2$	-1/3					
e	0.511 MeV/c ²	-1					
μ	105.7 MeV/c ²	-1					
τ	1.777 GeV/c ²	-1					
ν_e	<2.2 eV/c ²	0					
ν_μ	<0.17 MeV/c ²	0					
ν_τ	<15.5 MeV/c ²	0					
W	80.4 GeV/c ²	± 1					

CC BY 3.0 Wikipedia users MissMJ, Nasfarley88, et al.

But what comes next?

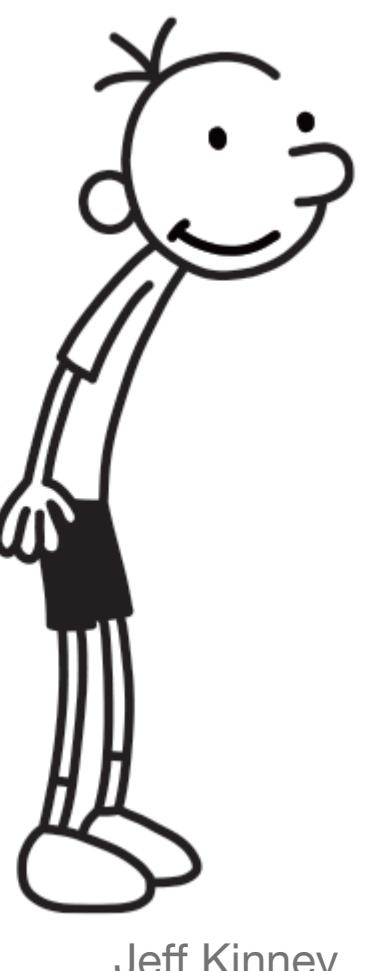
Beyond the Standard Model?



[Francisco de Goya](#)



Technicolor Group



Jeff Kinney

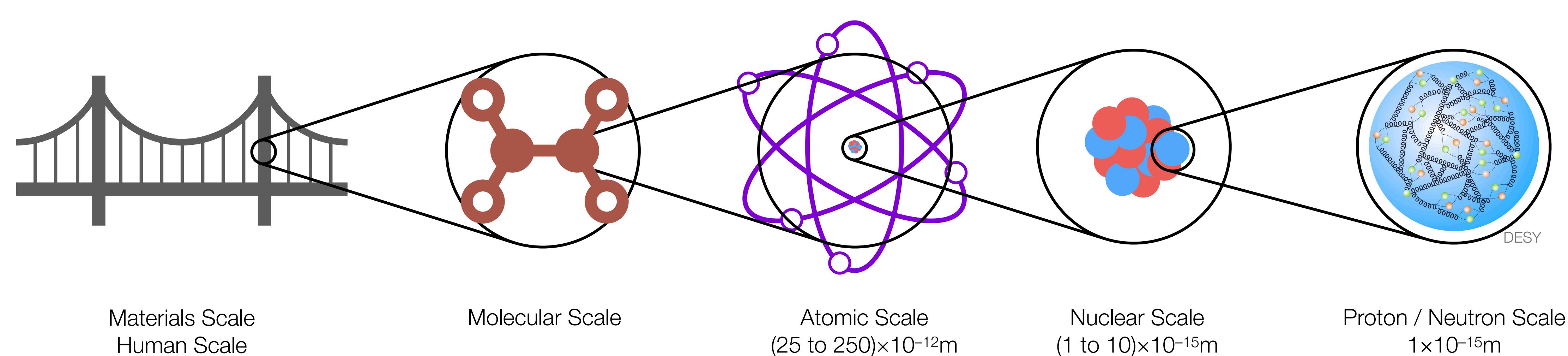


[Getty Images iStock / Alexandrum 79](#)

Standard Model as an EFT

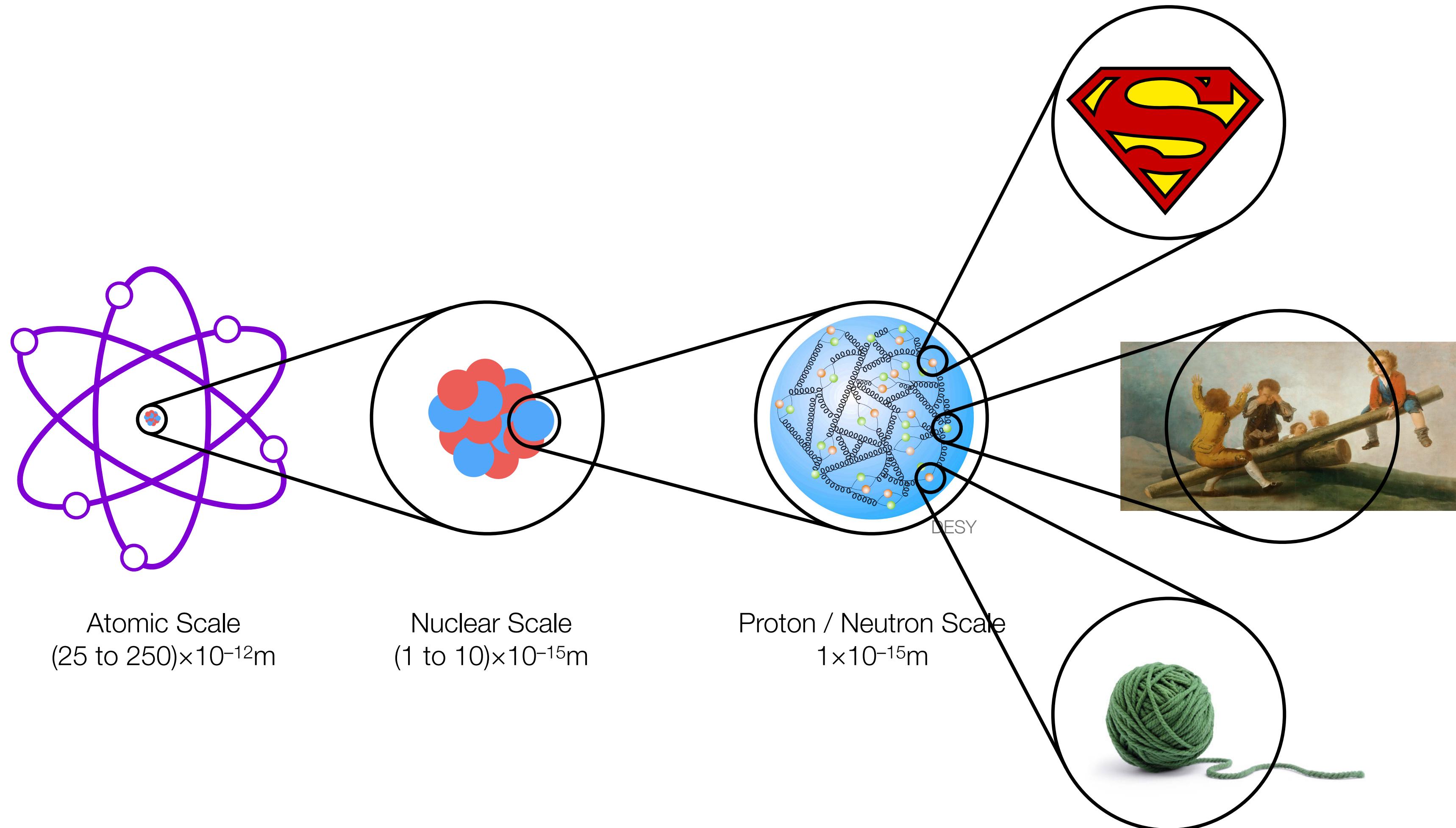
- We can summarize BSM models by the effects they have on the Standard Model
- The most obvious new effects will be ones where 'fundamental' symmetries are violated!
- Experiments search for these + can't get confused because the SM background is 0!

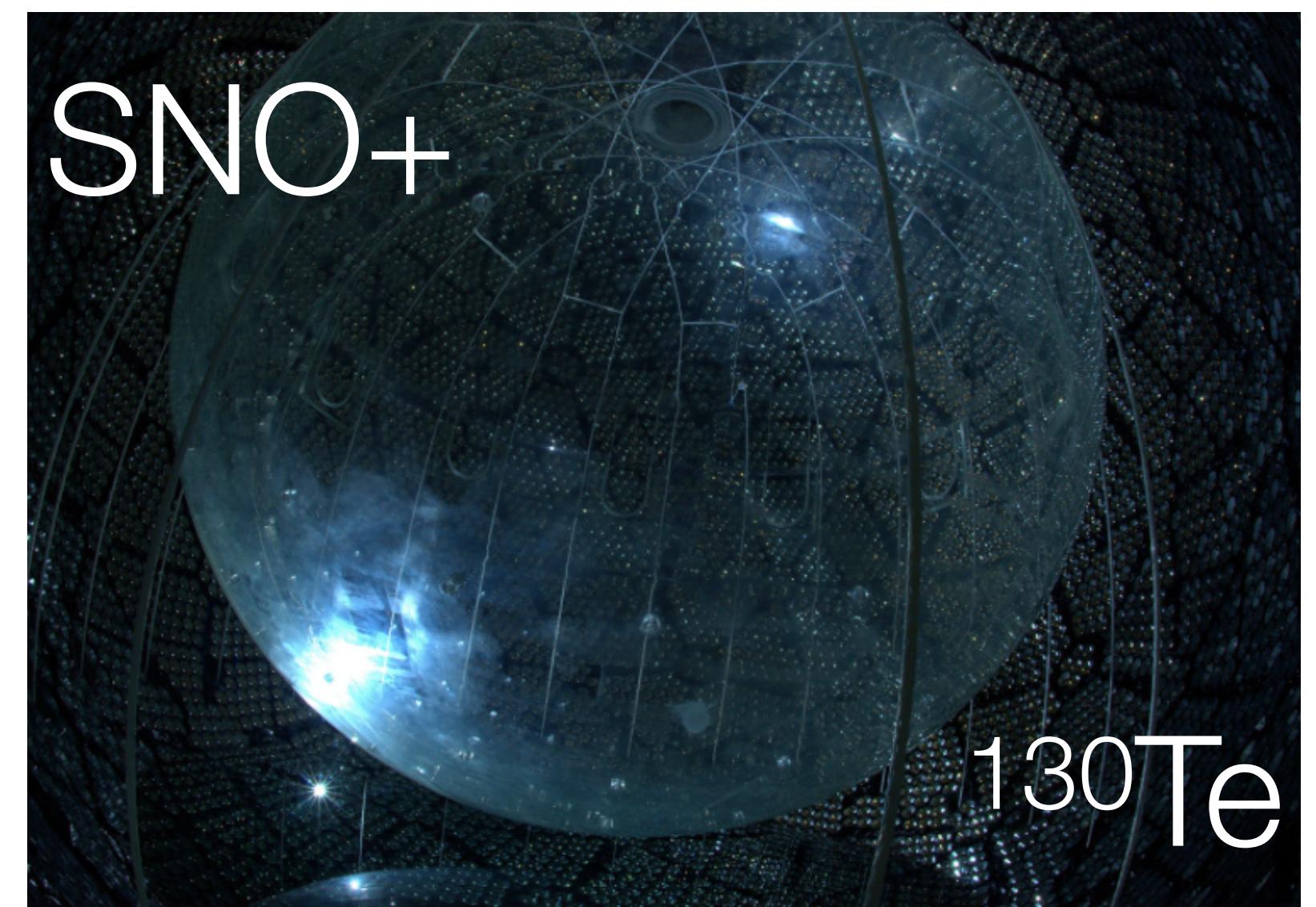
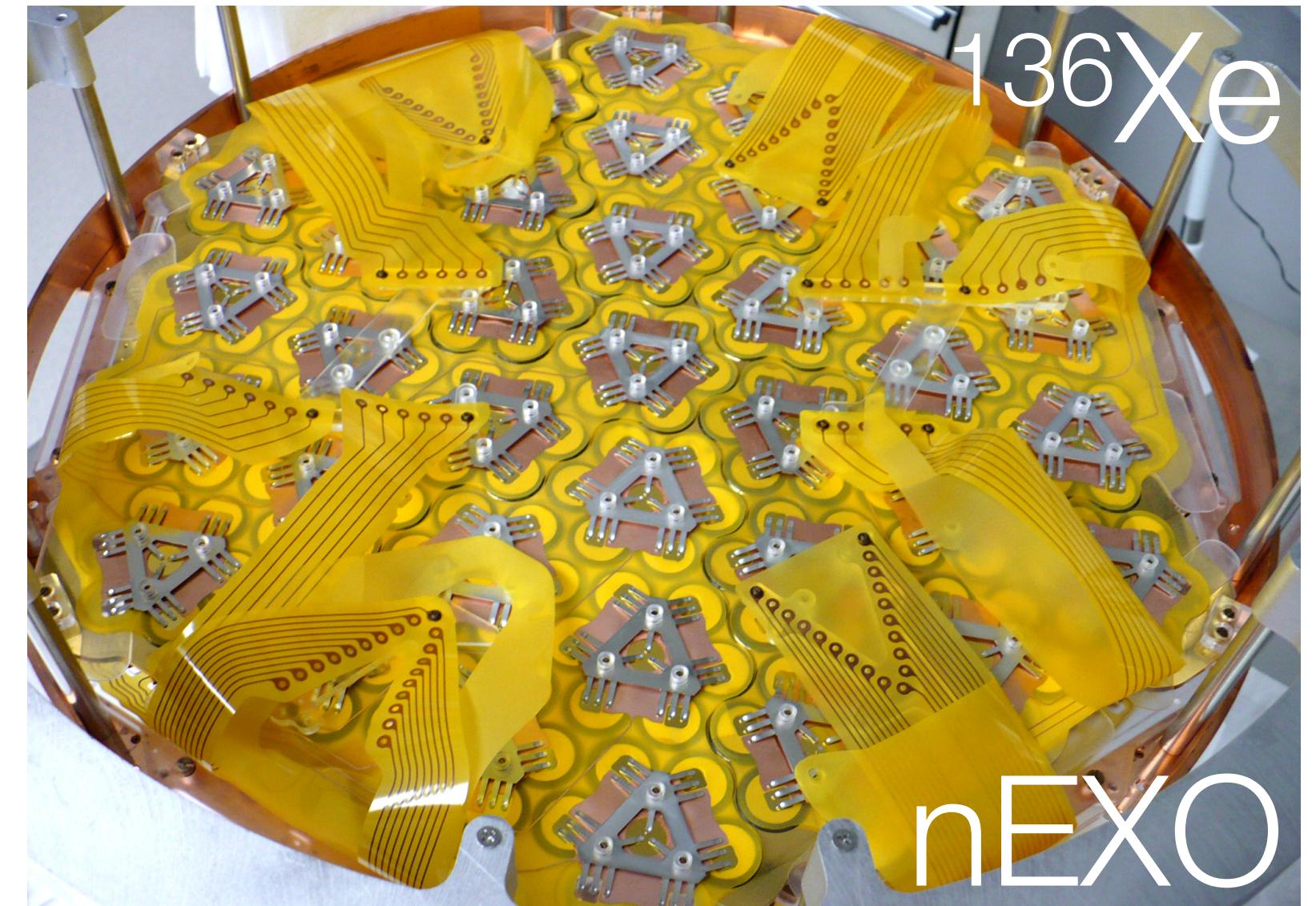
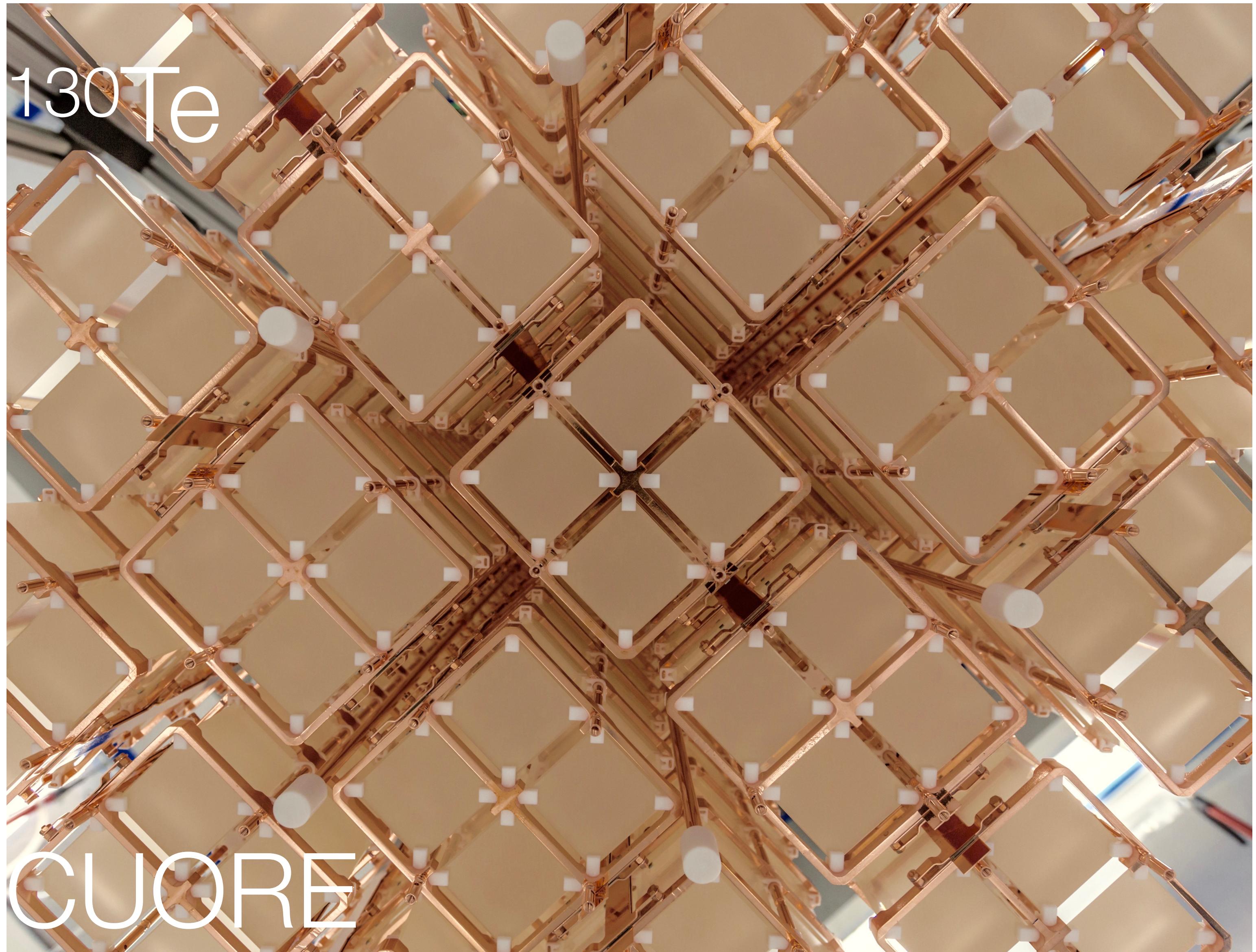
'Separation of scales'



Standard Model as an EFT

What if...?





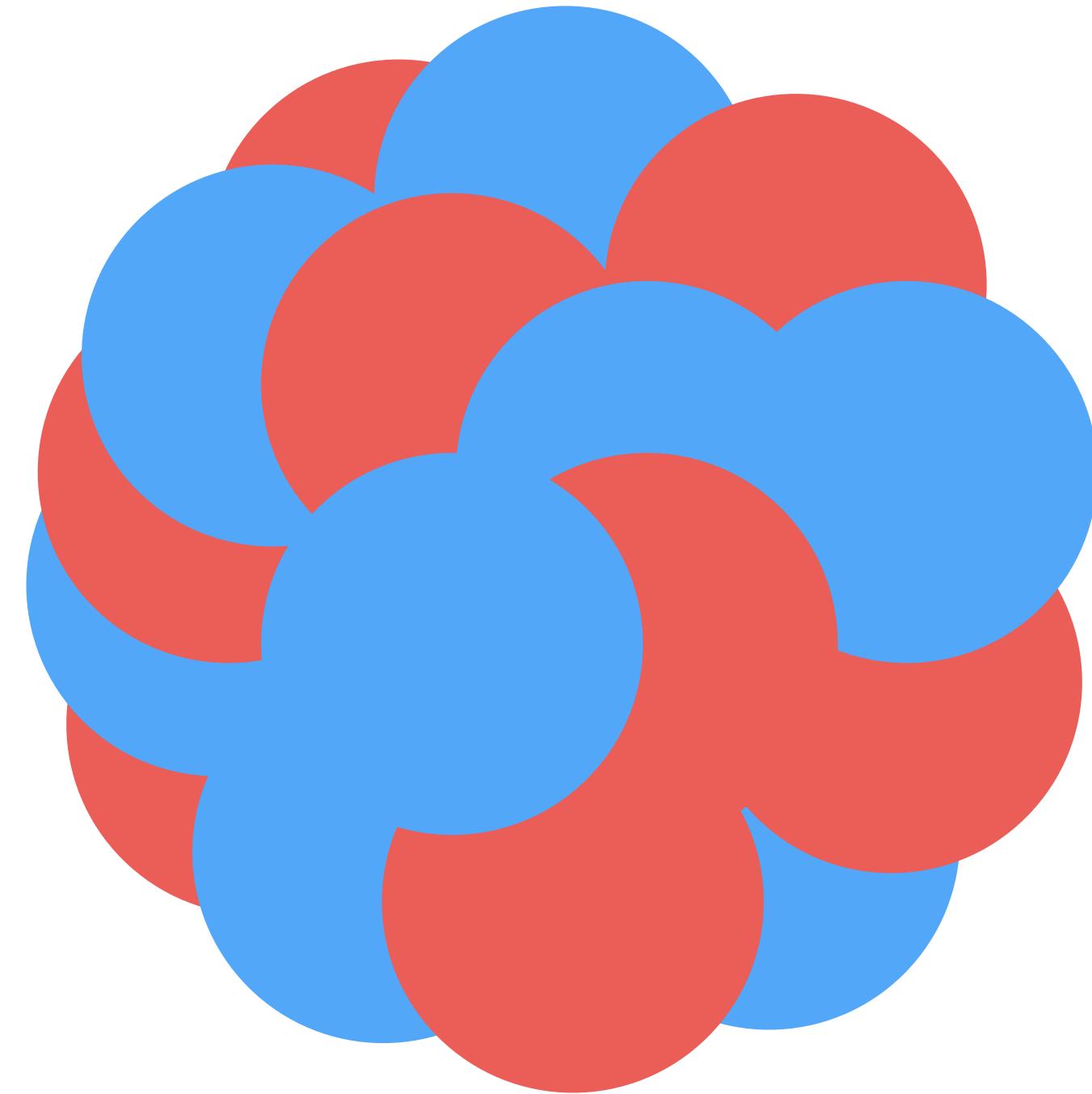
Hunting Lepton Number Violation

Double β Decay and Lepton Number Violation



nobelprize.org

Goeppert Mayer 1935

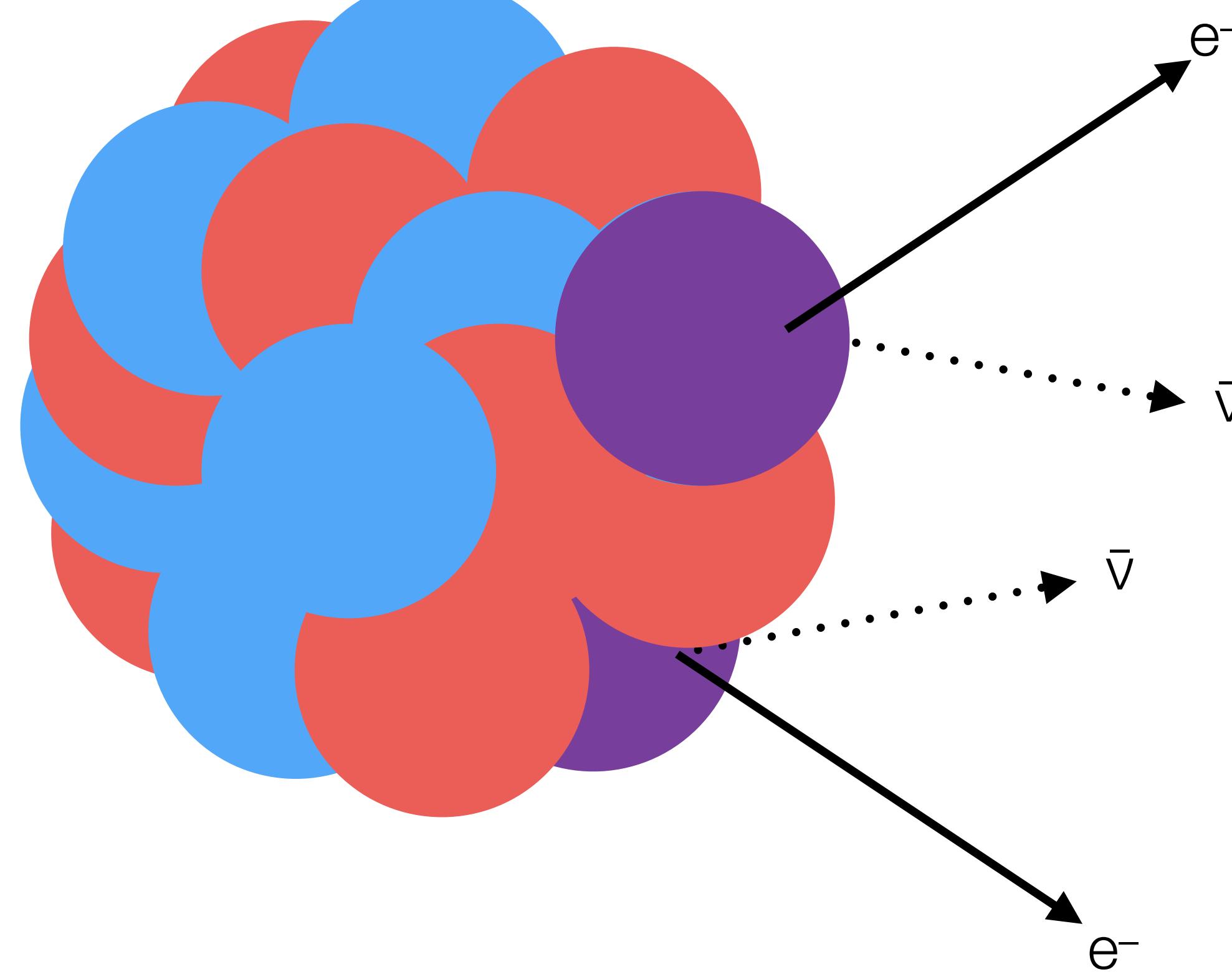


Double β Decay and Lepton Number Violation



nobelprize.org

Goeppert Mayer 1935

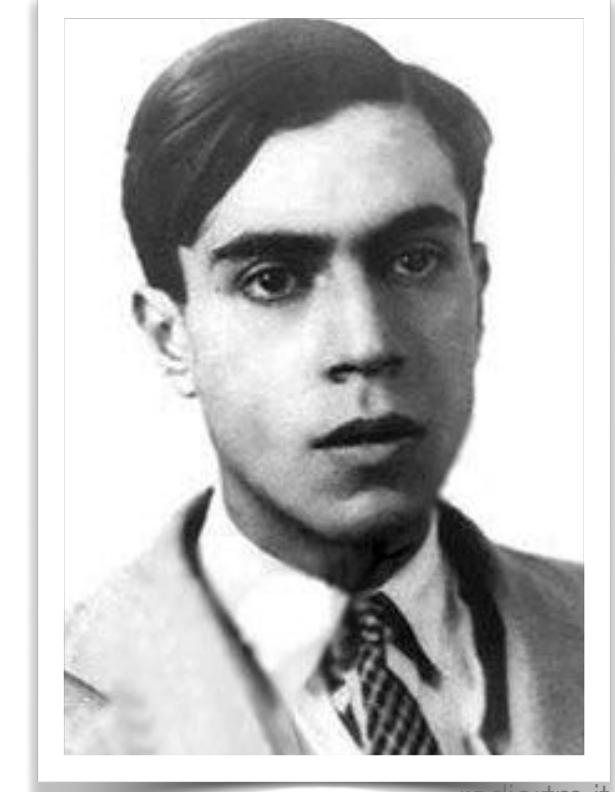
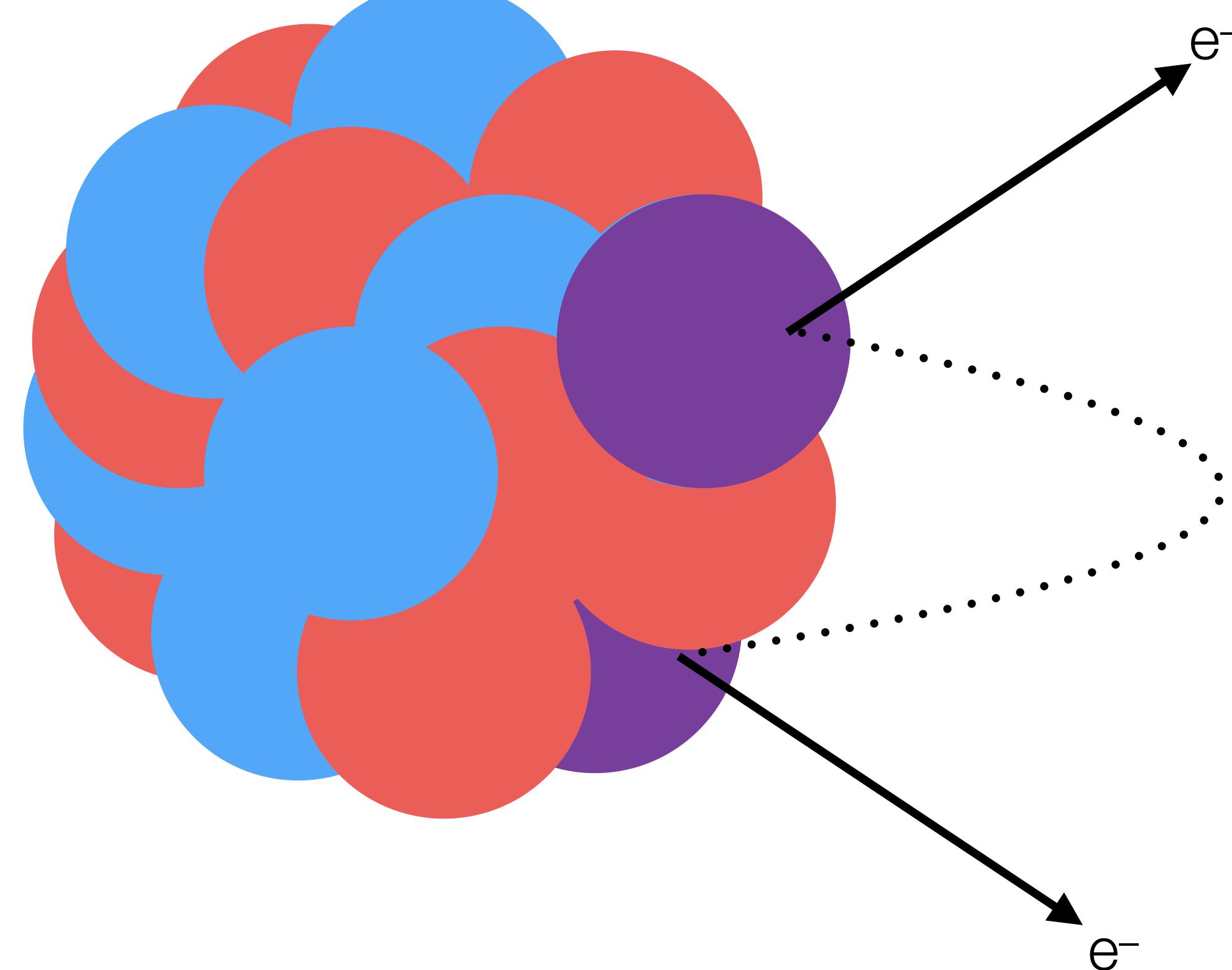


Double β Decay and Lepton Number Violation



nobelprize.org

Goeppert Mayer 1935



radiotm.it

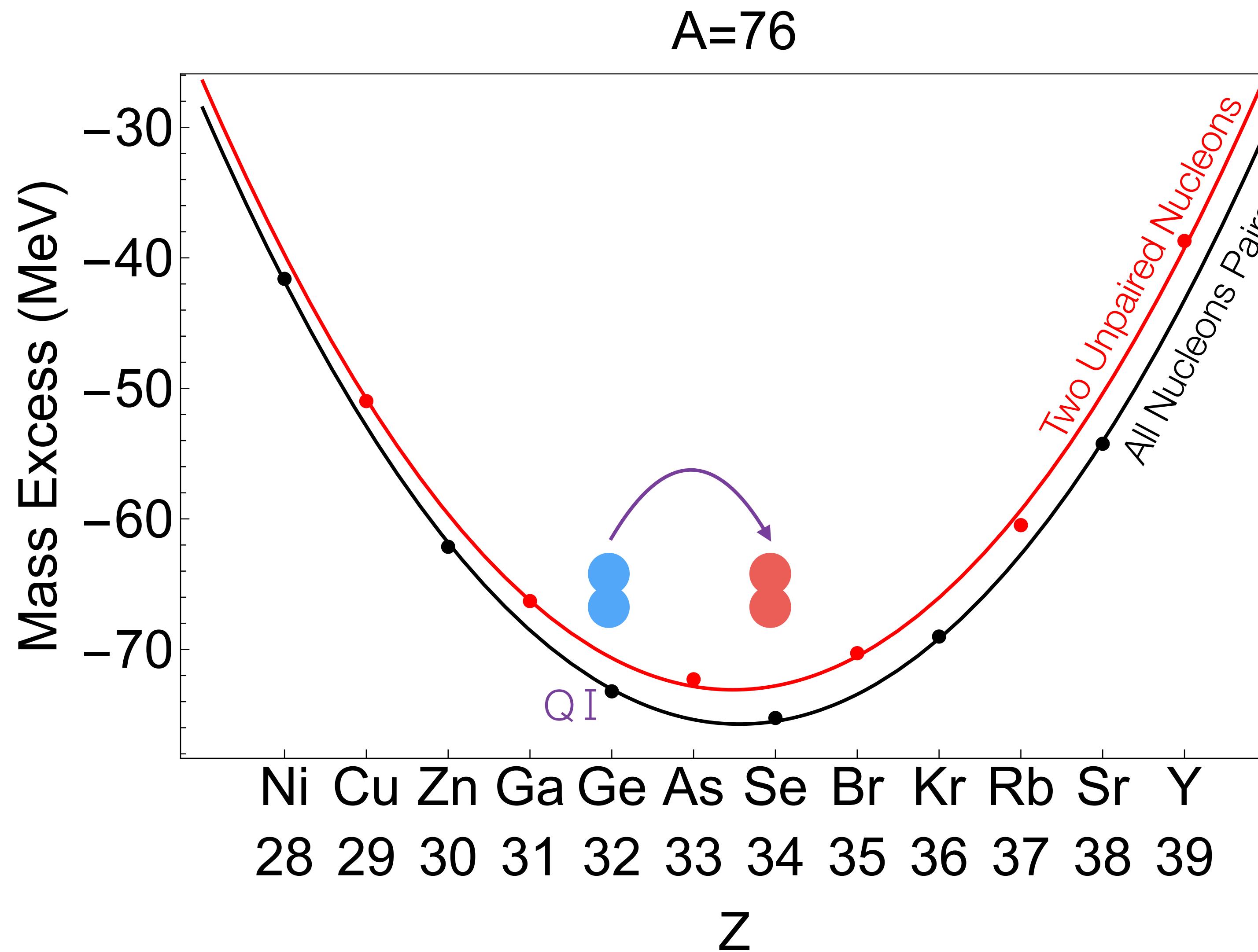
Majorana 1937



alchetron.com

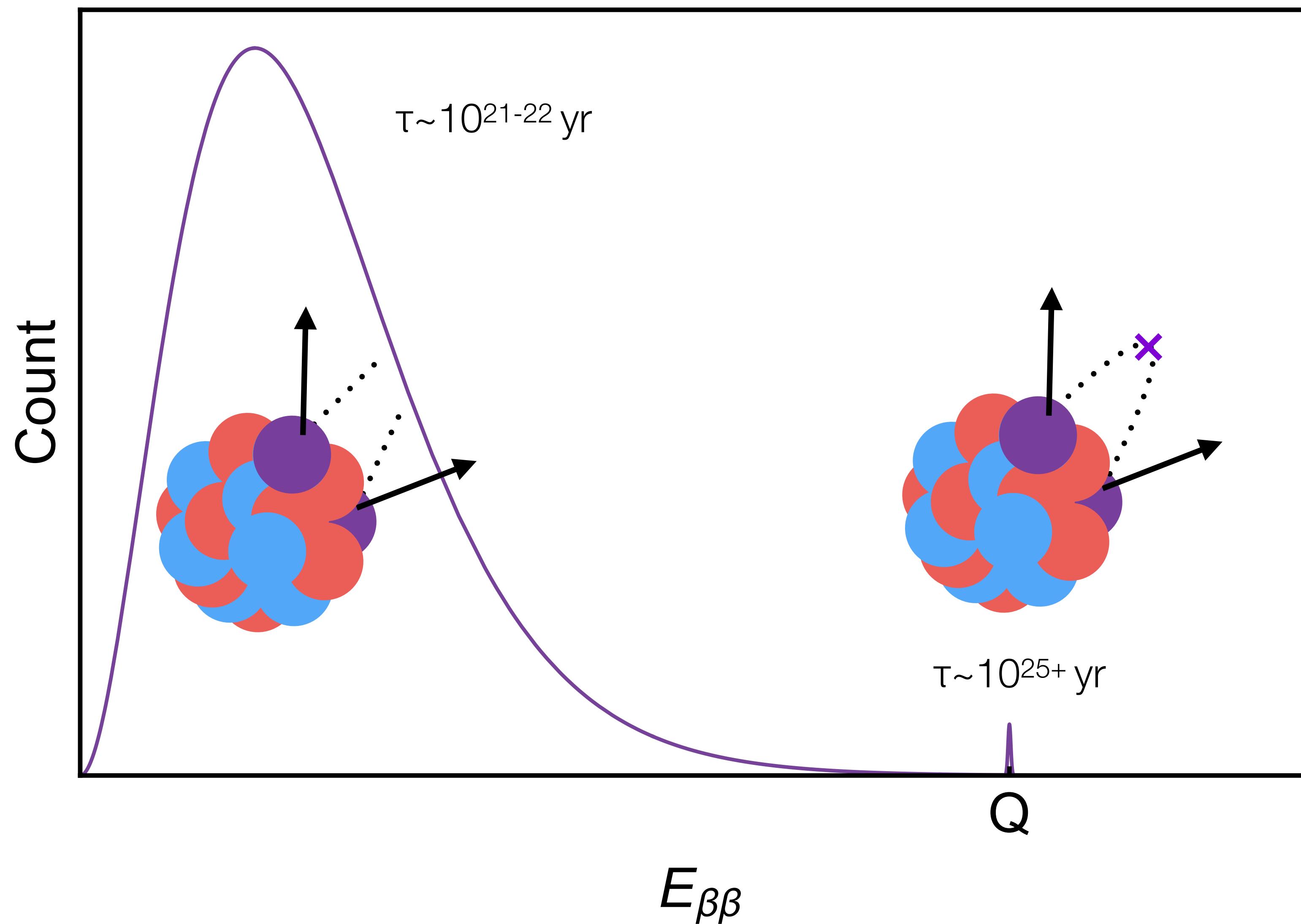
Furry 1939

Nuclear Laboratory

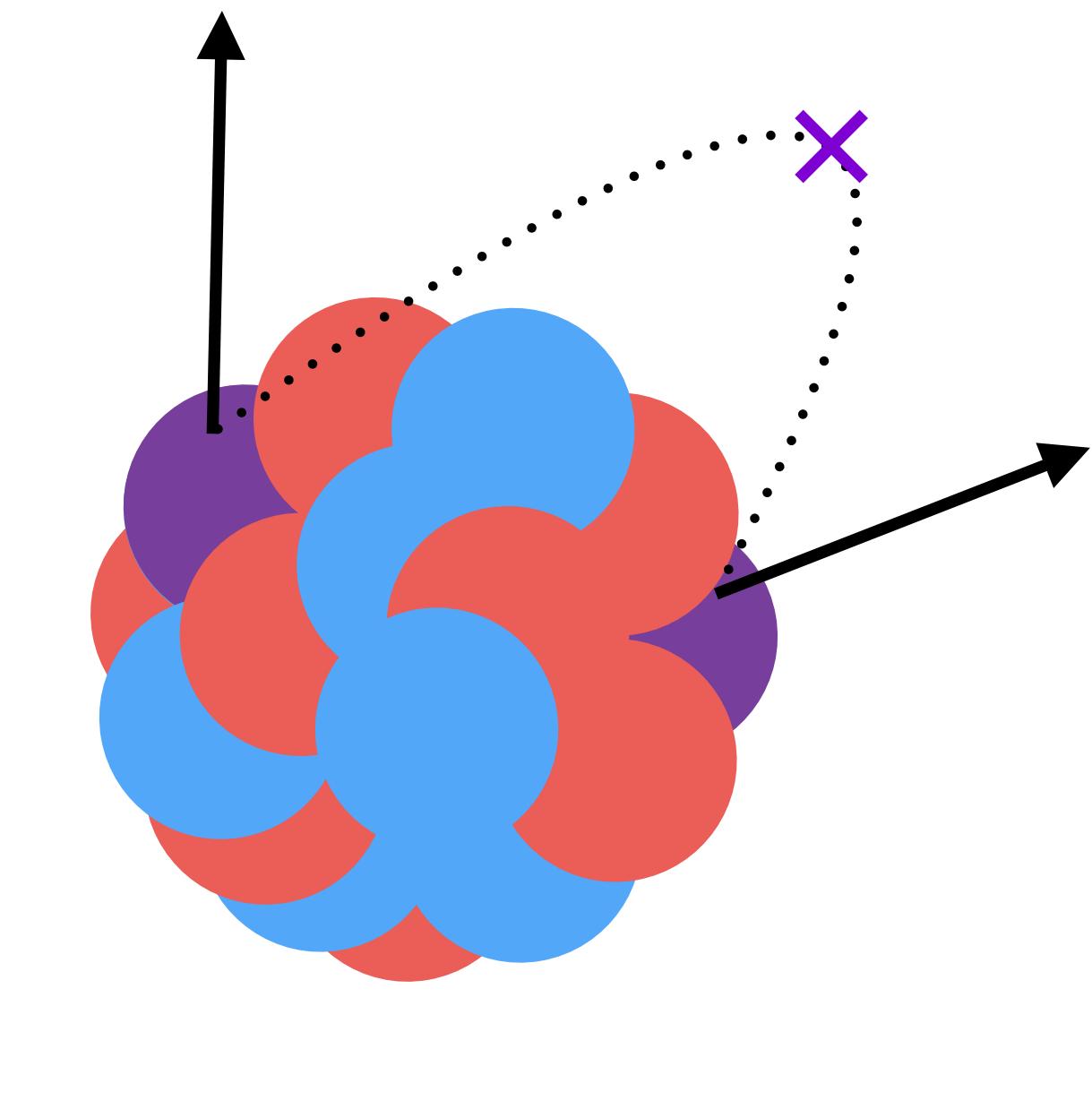
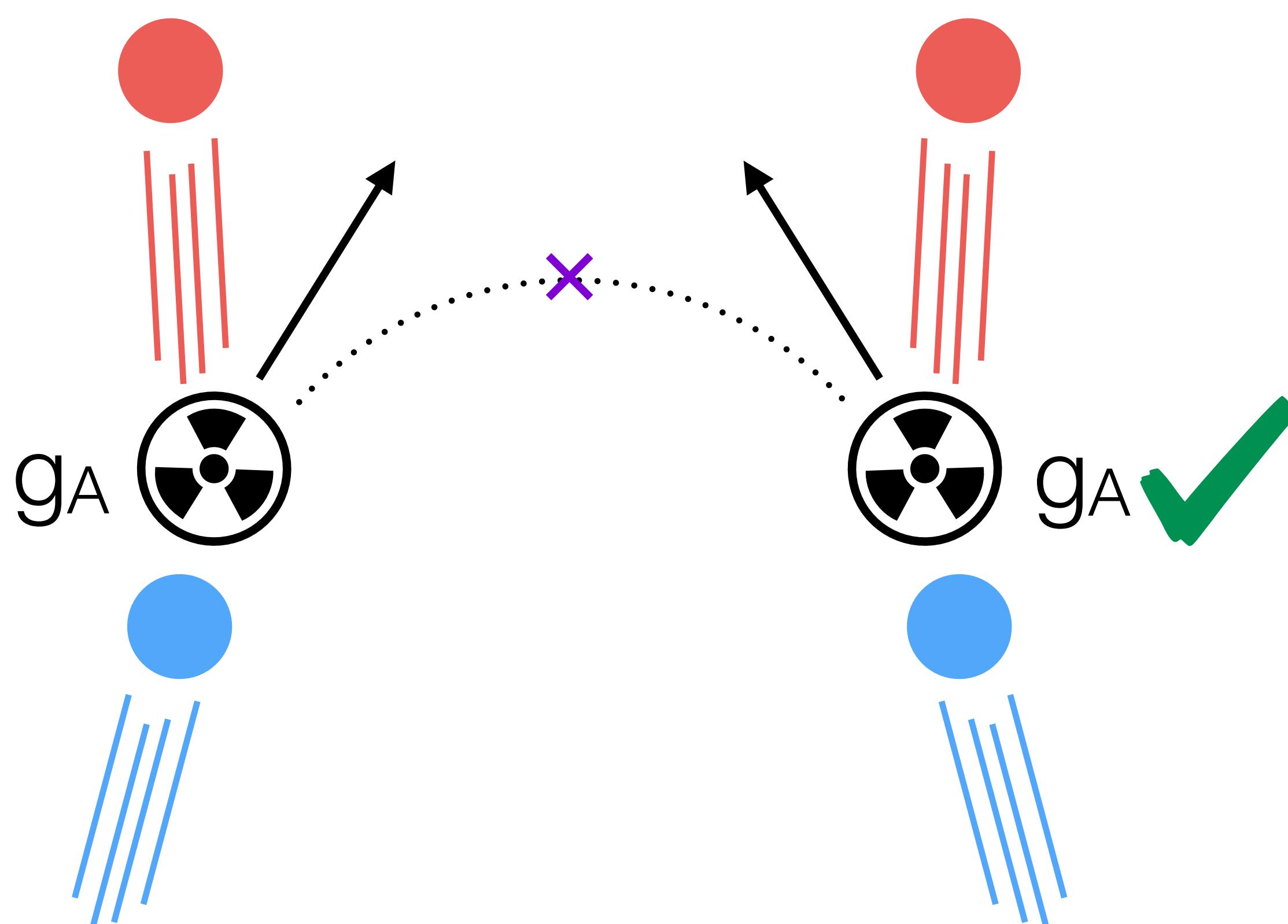
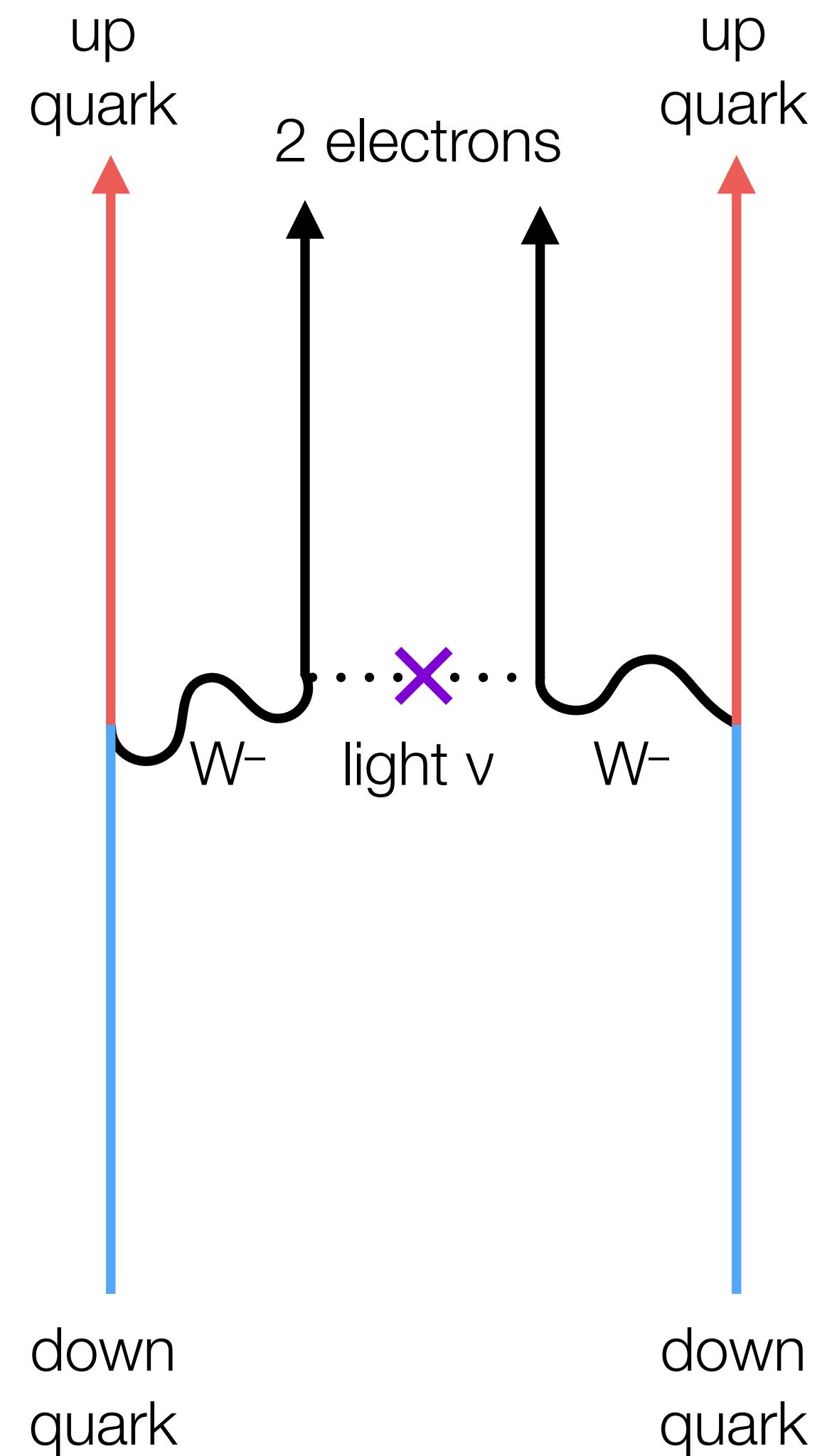


- Energetically impossible to have a single decay, but possible to have two simultaneous decays.
- Energy of the leptons sums to Q .

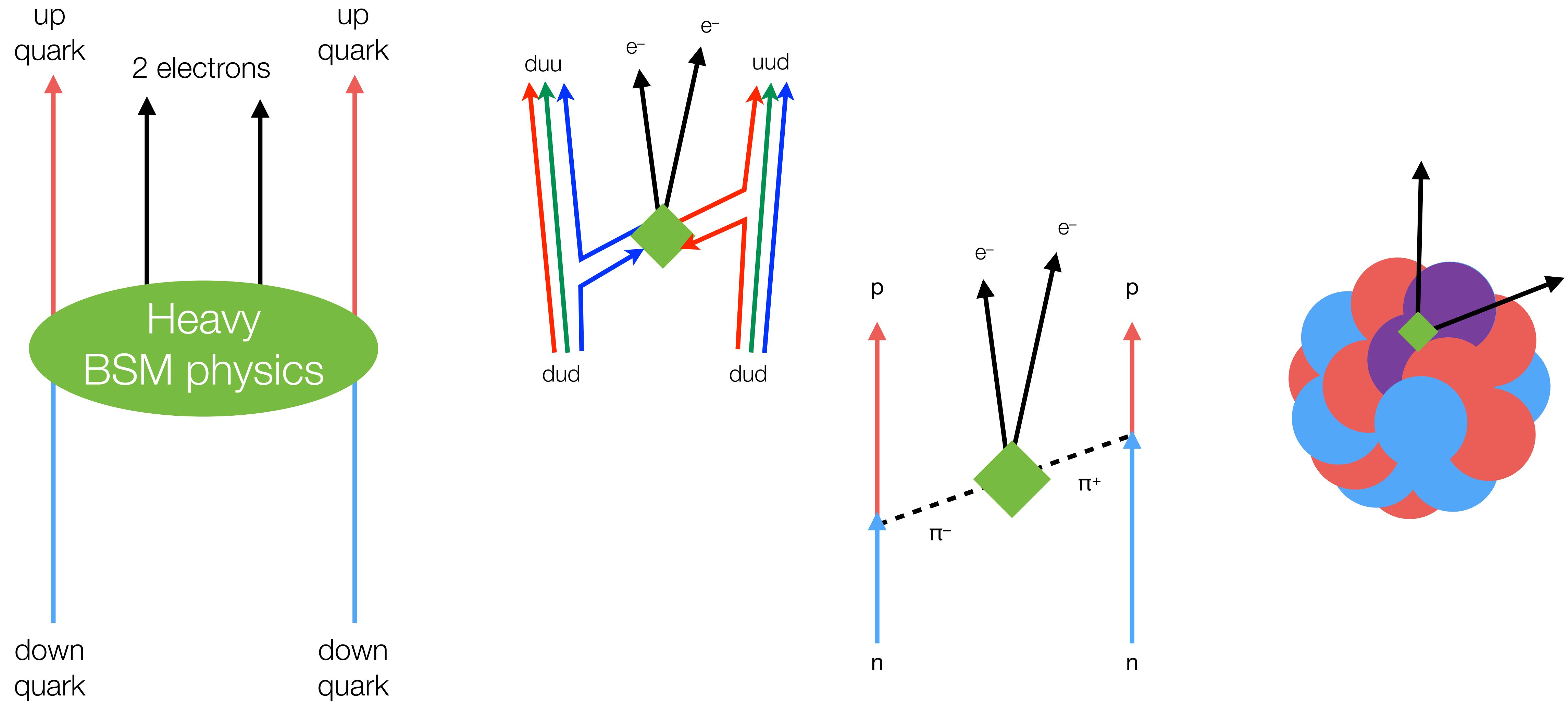
Decay Rates



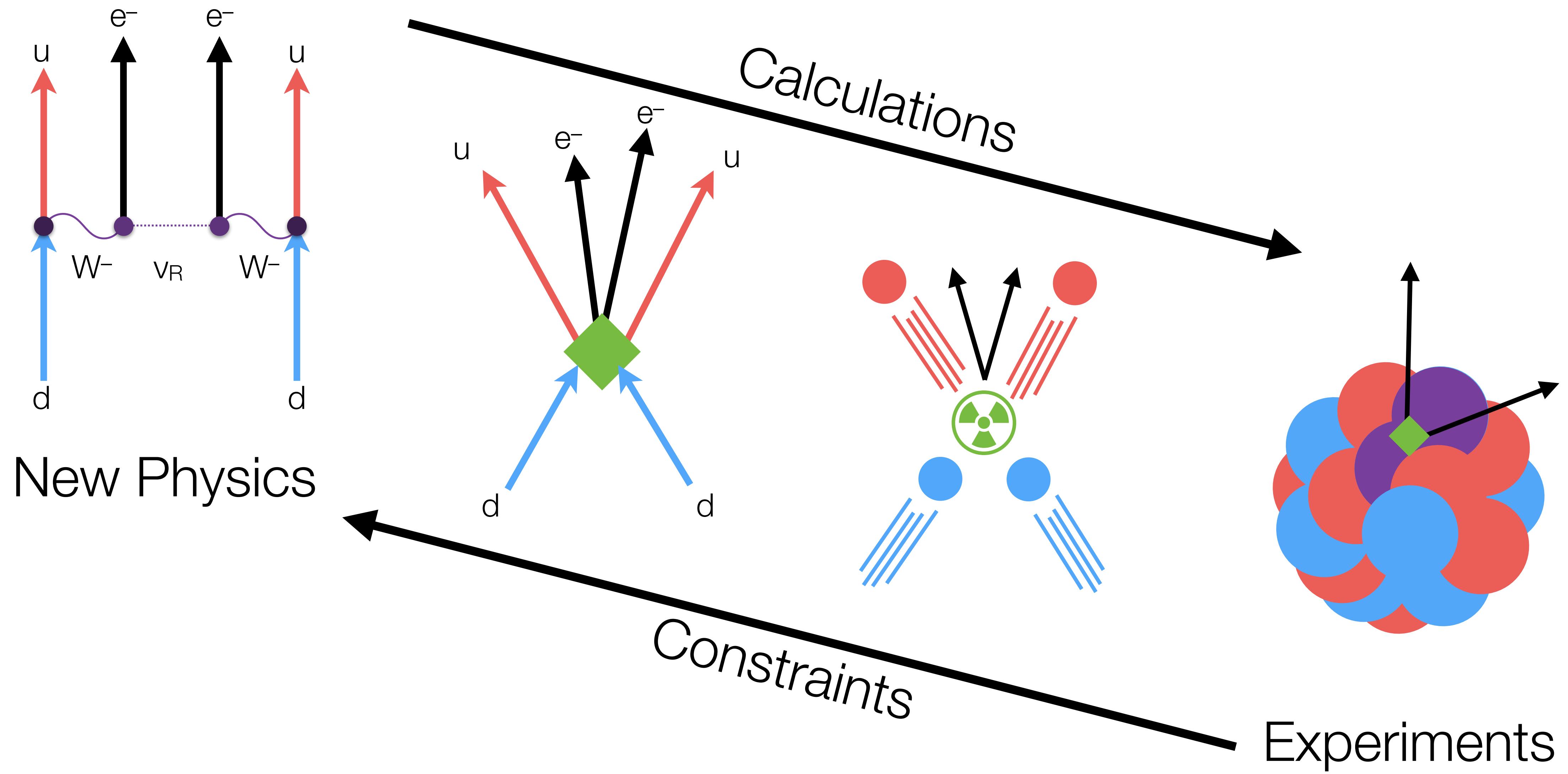
Neutrinoless Double Beta Decay $0\nu\beta\beta$



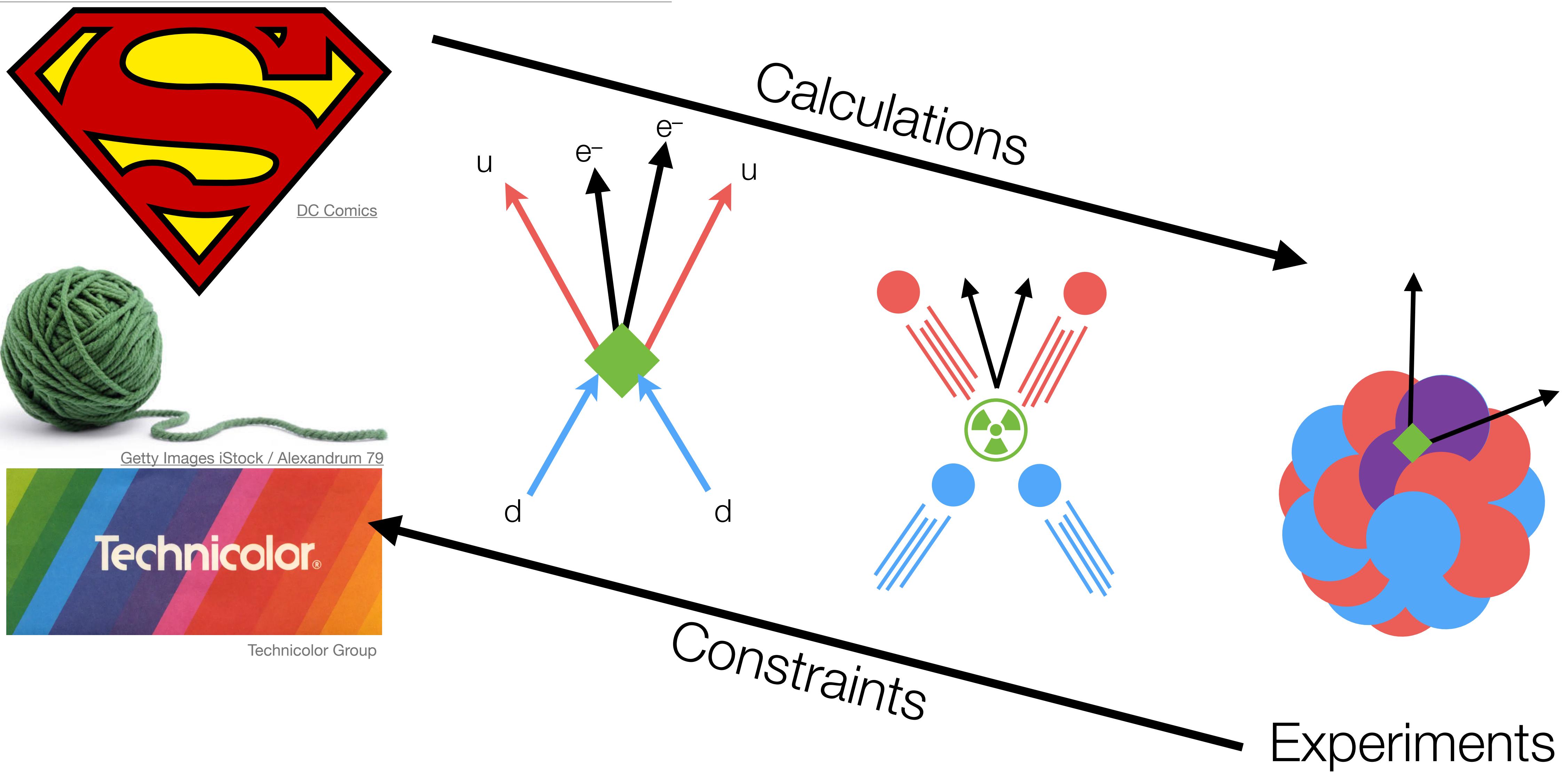
Neutrinoless Double Beta Decay $0\nu\beta\beta$



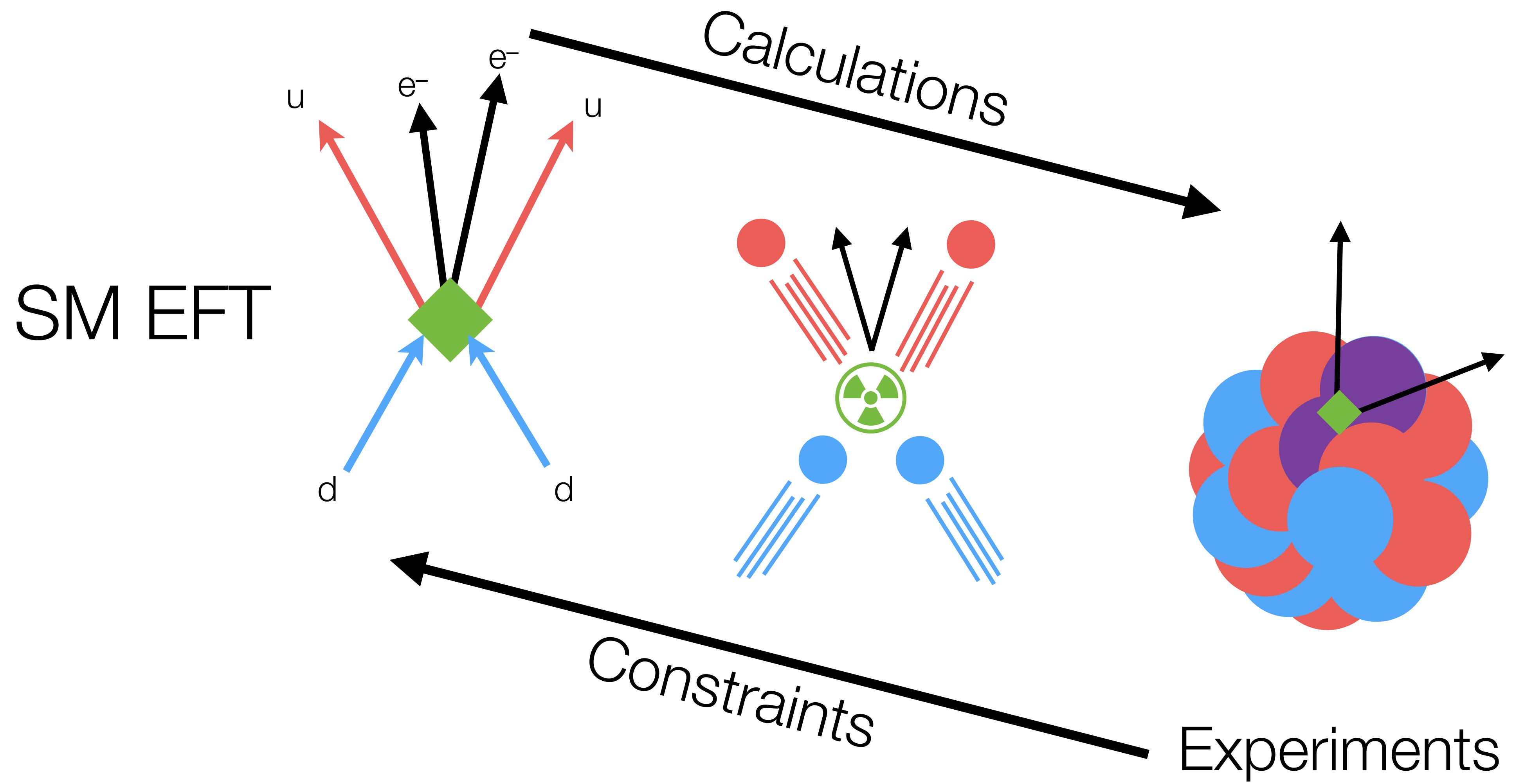
Nuclear Laboratories



Nuclear Laboratories

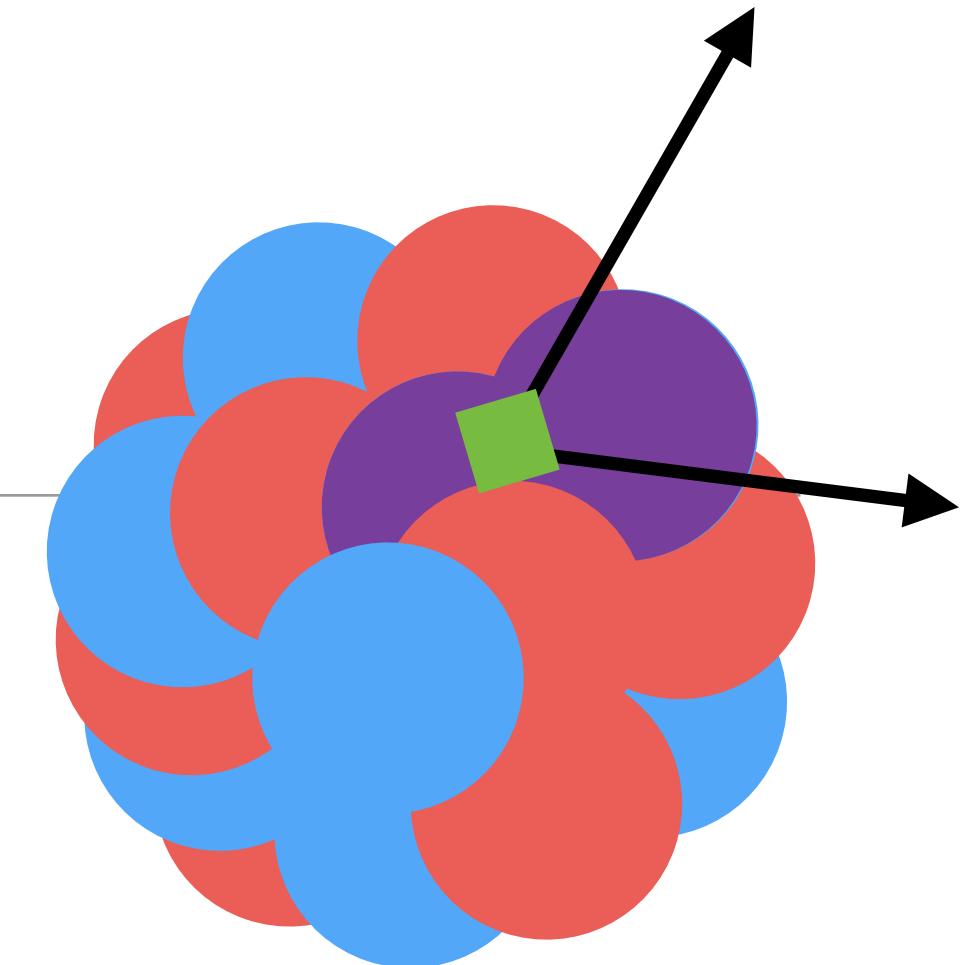
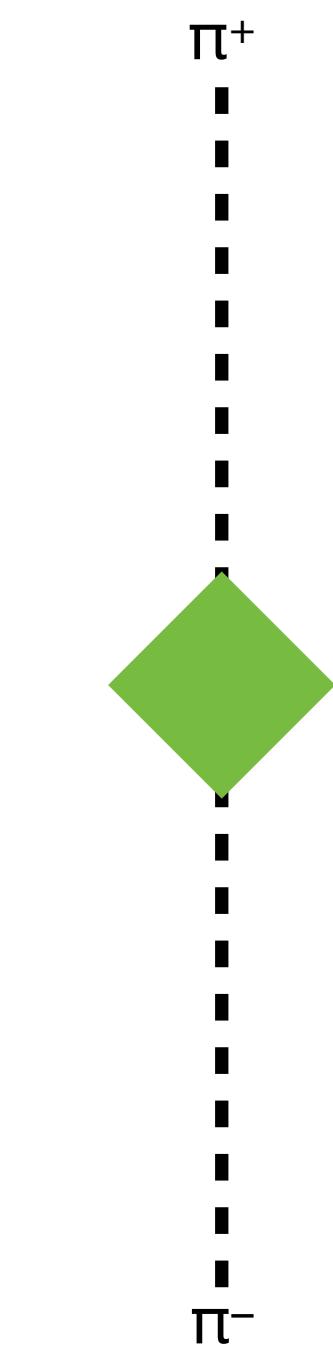
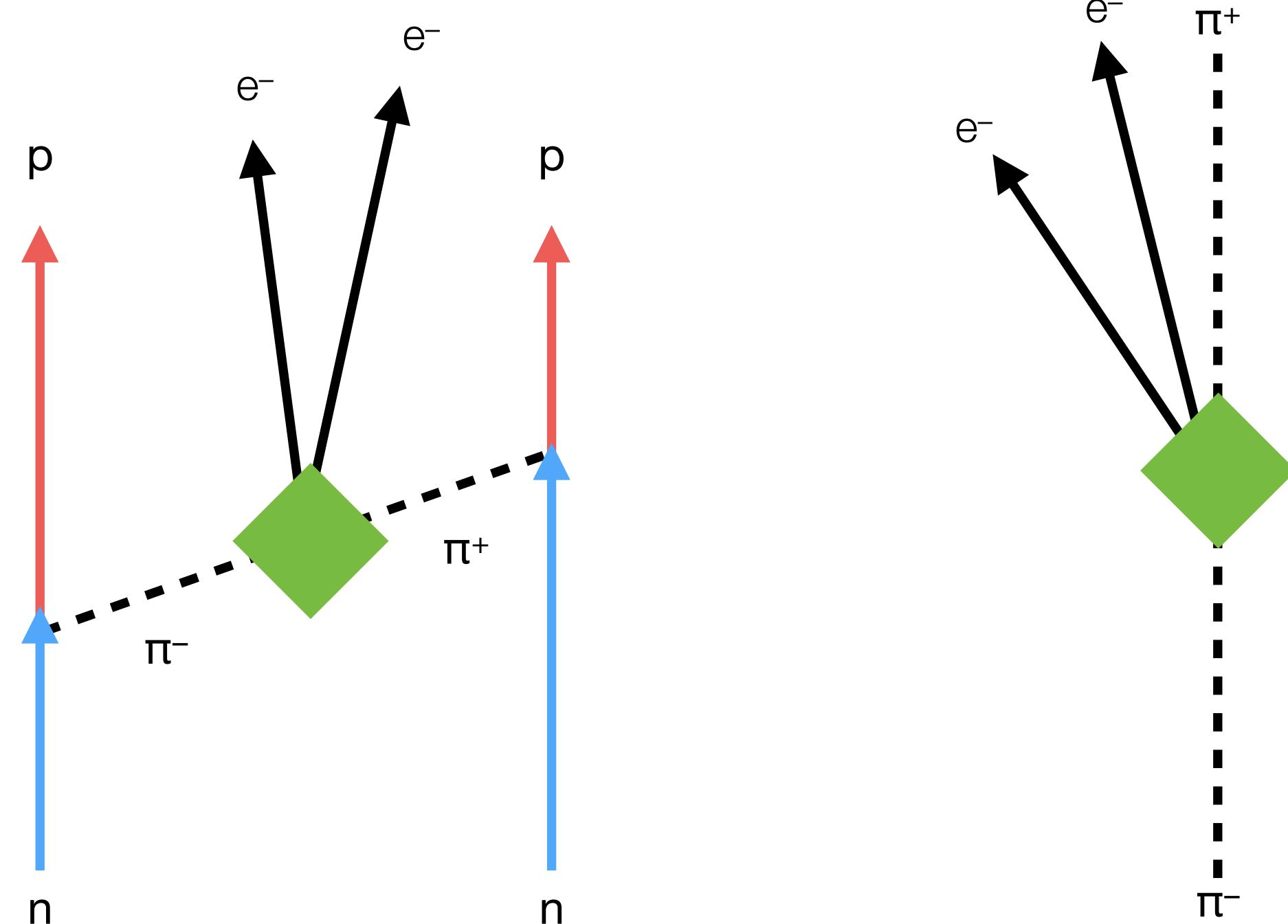


Add fundamental-symmetry-violating terms to the SM



Simplify, simplify, simplify!

Prézeau, Ramsey-Musolf, Vogel PRD68 (2003) 034016 hep-ph/0303205

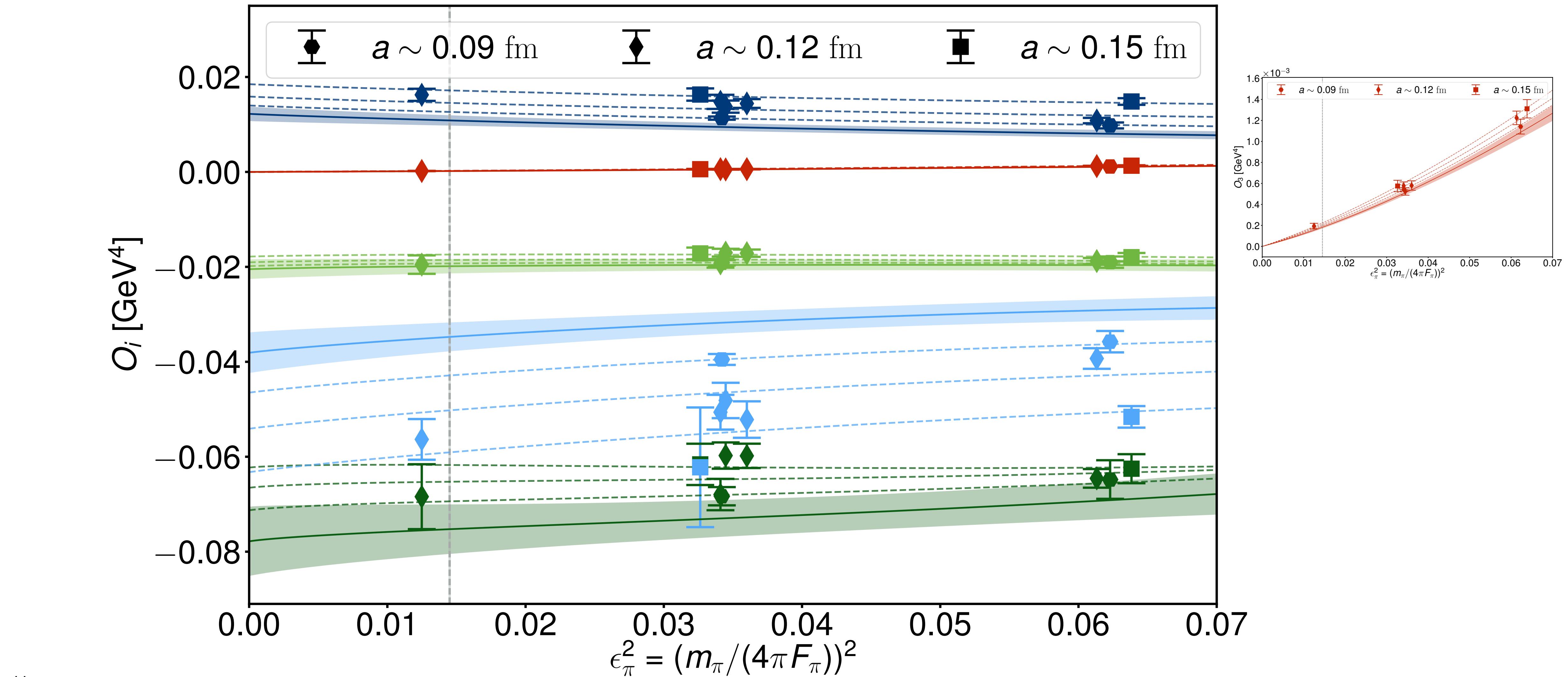
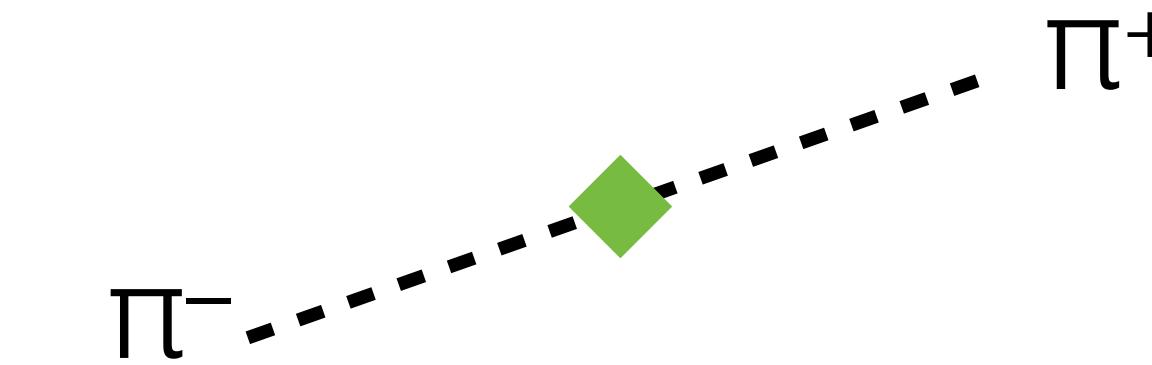


- 💡 These are *the simplest* hadronic matrix elements, computationally.
- 💡 They're also the most important for short-distance $0\nu\beta\beta$!
- 💡 My algorithm unlocked continuum, physical-point, infinite-volume results in the very first publication!

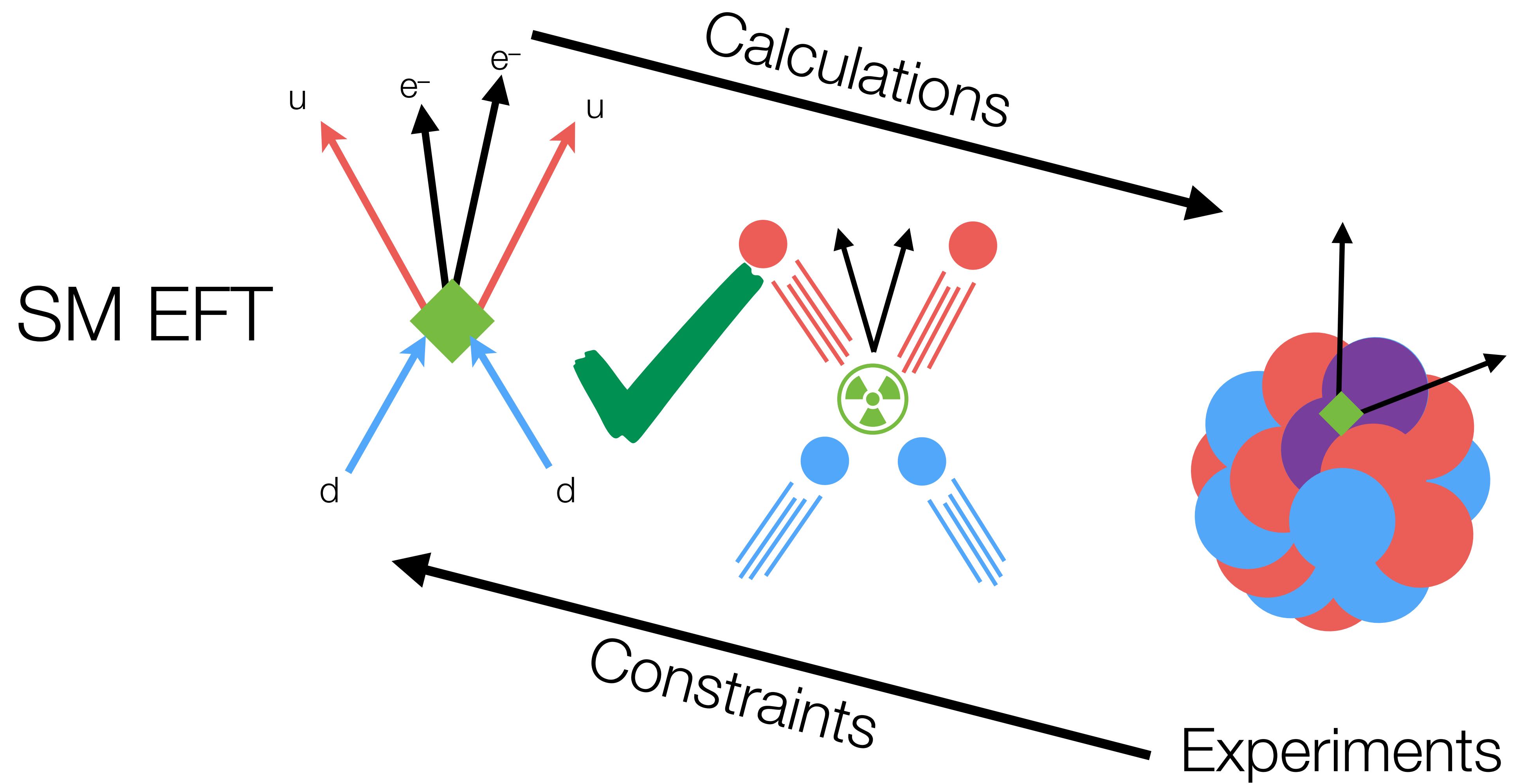
Nicholson **EB** et al., PRL 121:172501 (2018) arXiv:1805.02634

0νββ $\pi^- \rightarrow \pi^+ ee$ Transition

Nicholson **EB** et al., PRL 121:172501 (2018) arXiv:1805.02634



Add fundamental-symmetry-violating terms to the SM



Recap

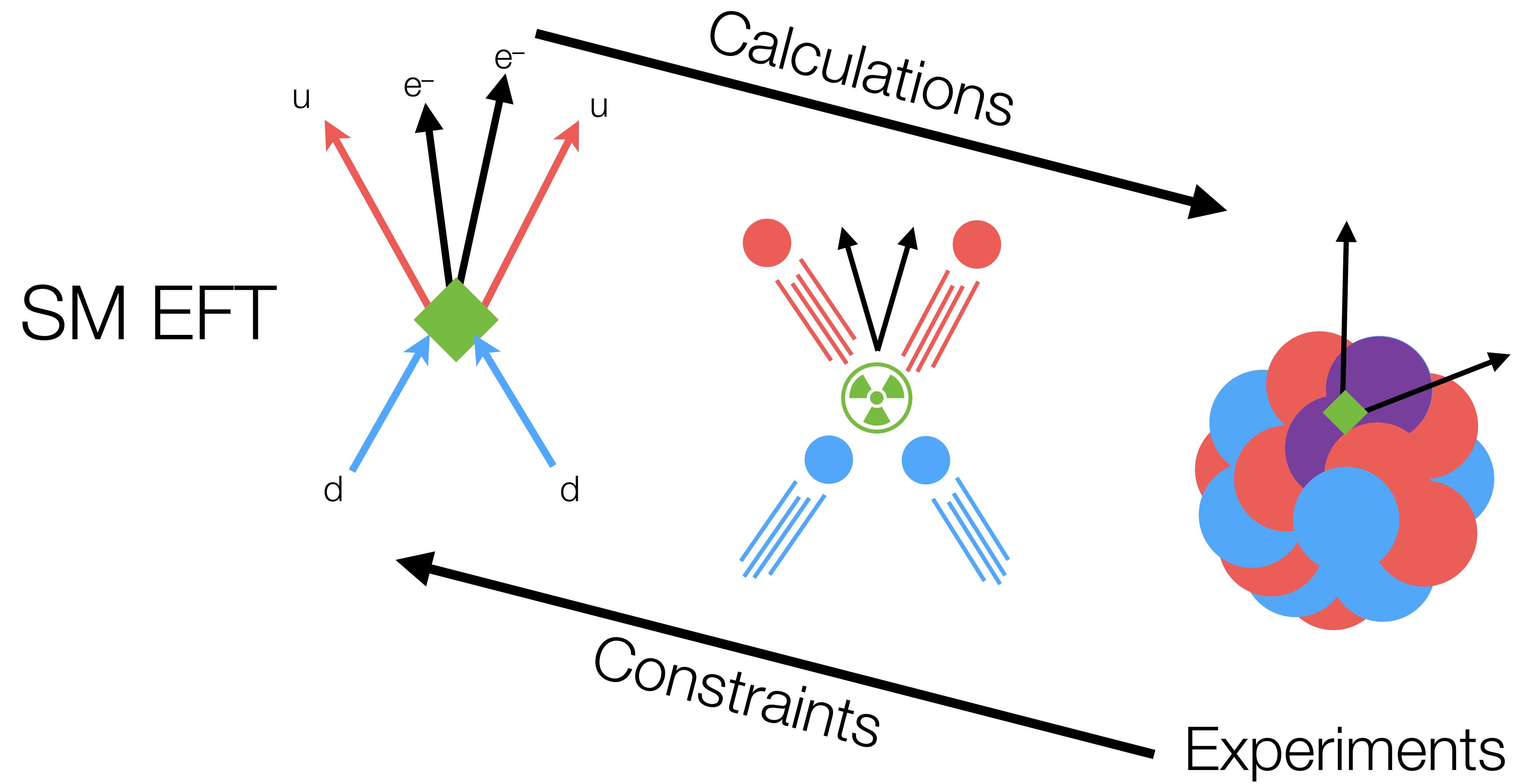
Effective Field Theory: include violations of 'fundamental' SM symmetries in a controlled way



	mass \rightarrow	charge \rightarrow	spin \rightarrow	
QUARKS				
u	$\approx 2.3 \text{ MeV}/c^2$	$2/3$	$1/2$	up
c	$\approx 1.275 \text{ GeV}/c^2$	$2/3$	$1/2$	charm
t	$\approx 173.07 \text{ GeV}/c^2$	$2/3$	$1/2$	top
g	0	0	1	gluon
H	$\approx 126 \text{ GeV}/c^2$	0	0	Higgs boson
LEPTONS				
d	$\approx 4.8 \text{ MeV}/c^2$	$-1/3$	$1/2$	down
s	$\approx 95 \text{ MeV}/c^2$	$-1/3$	$1/2$	strange
b	$\approx 4.18 \text{ GeV}/c^2$	$-1/3$	$1/2$	bottom
e	$0.511 \text{ MeV}/c^2$	-1	$1/2$	electron
μ	$105.7 \text{ MeV}/c^2$	-1	$1/2$	muon
τ	$1.777 \text{ GeV}/c^2$	-1	$1/2$	tau
ν_e	$<2.2 \text{ eV}/c^2$	0	$1/2$	electron neutrino
ν_μ	$<0.17 \text{ MeV}/c^2$	0	$1/2$	muon neutrino
ν_τ	$<15.5 \text{ MeV}/c^2$	0	$1/2$	tau neutrino
GAUGE BOSONS				
Z	$91.2 \text{ GeV}/c^2$	0	1	Z boson
W	$80.4 \text{ GeV}/c^2$	± 1	1	W boson

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Understanding Experiments Requires Understanding the SM



Understanding the SM Requires LQCD

